

# *Magnetic property characterisation focusing on soil and archaeological materials.*



***Training school TS3  
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Framework Programme of the  
European Union

- *Properties of some magnetic minerals*
- *Formation of magnetic minerals*
- *Magnetic characterisation methods*
- *Examples*

Element Abundance (wt %)\*  
in Earth's crust

\*Lutgens & Tarbuck 2000

Element	Abundance (wt %)*	Magnetite	$\text{Fe}_3\text{O}_4$
<b>Oxygen</b>	<b>46.6</b>	Maghaemite	$\gamma\text{-Fe}_2\text{O}_3$
Silicon	27.7	Haematite	$\alpha\text{-Fe}_2\text{O}_3$
Aluminum	8.1	Goethite	$\alpha\text{-FeOOH}$
<b>Iron</b>	<b>5.0</b>	Pyrrhotite	mon. $\text{Fe}_7\text{S}_8$ hex. $\text{Fe}_9\text{S}_{10}$
Calcium	3.6	Greigite	$\text{Fe}_3\text{S}_4$
Sodium	2.8		
Potassium	2.6		
Magnesium	2.1		
All other	1.5		

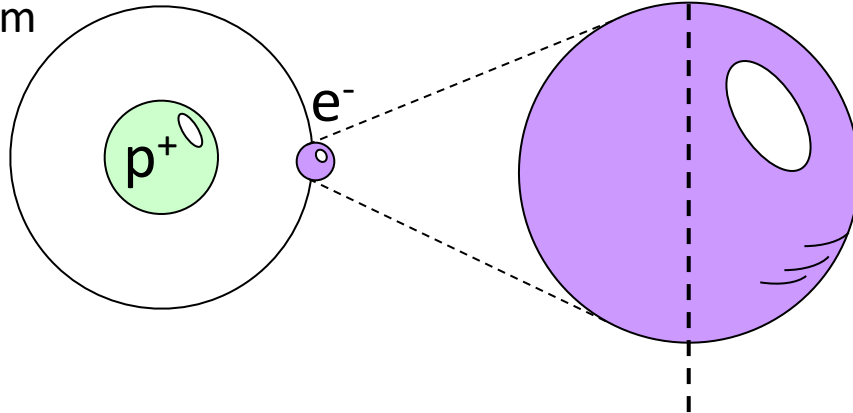
**Iron** resides amongst the most abundant elements in the Earth's crust and forms in combination with **oxygen** and **sulphur** magnetic minerals which are omnipresent in our environment.

## Electrons = moving electric charges

Nucleus with orbiting electron

Spinning electron

H-atom



Orbital angular momentum

Spin angular momentum

$$\mu_{orbit} = -\frac{e n \hbar}{2m}$$

$$\mu_{spin} = -\frac{e S \hbar}{m}$$

$n$  – main quantum number of Hydrogen, charge,  $\hbar$  – reduced Planck constant,  $s$  – spin quantum number of  $e^-$ ,  $m$  – mass of  $e^-$ ,  $e$  – elementary

**Free atoms**

orbit + spin momenta

**Solids**

often only spin momenta

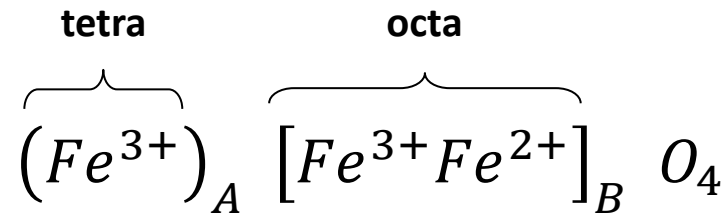
**Ferromagnetic s.l. minerals**

uncompensated spin momenta in overlapping orbits

## Magnetite

*ferrimagnetic*

- $Fe_3O_4$



$$M_S = 480 \text{ kA/m}$$

$$T_C = 585 \text{ }^\circ\text{C}$$

$$T_V = \text{between } -163 \text{ and } -153 \text{ }^\circ\text{C}$$

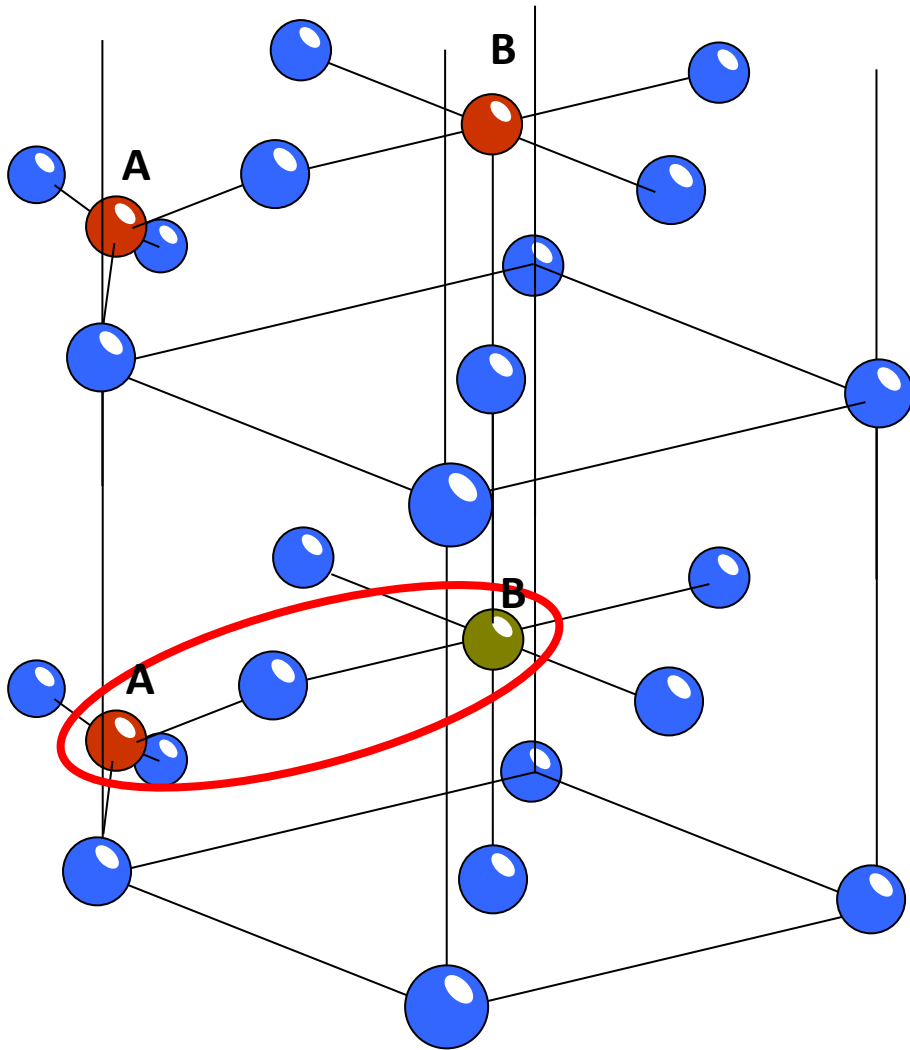
$$H_c = \text{between } 10 \text{ and } 80 \text{ mT}$$




(size dependent)

- (Soils)
- Inside bacteria
- Baked clays
- Combustion product
- Lacustrine/marine sediments

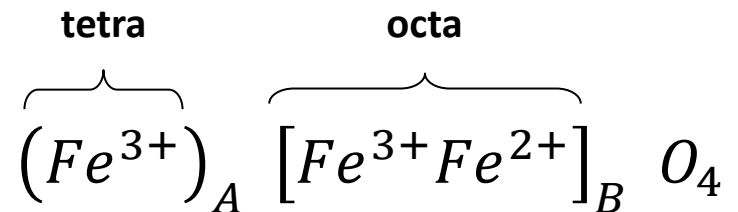


# Magnetic minerals



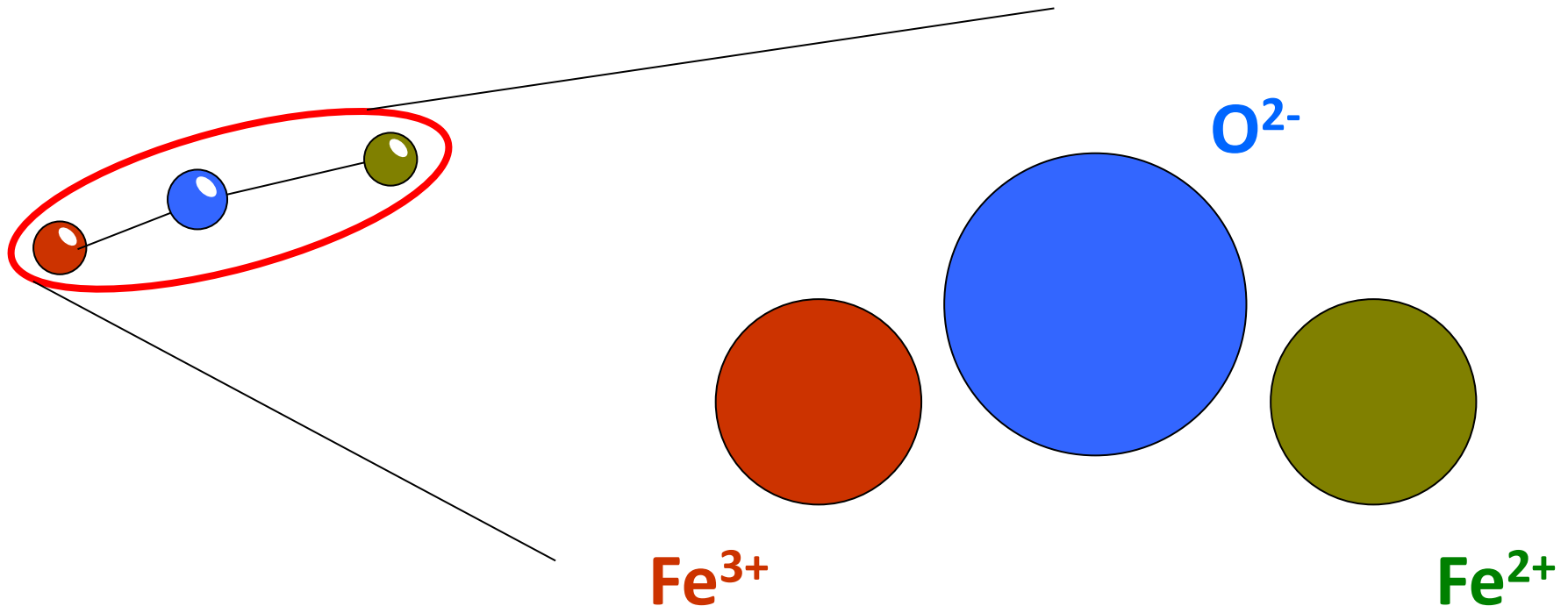
-  ferric iron Fe<sup>3+</sup> at tetrahedral (A) and octahedral (B) sites
-  ferrous iron Fe<sup>2+</sup> at octahedral site
-  oxygen anions

## Magnetite Fe<sub>3</sub>O<sub>4</sub>



# Superexchange

## *Magnetic minerals*

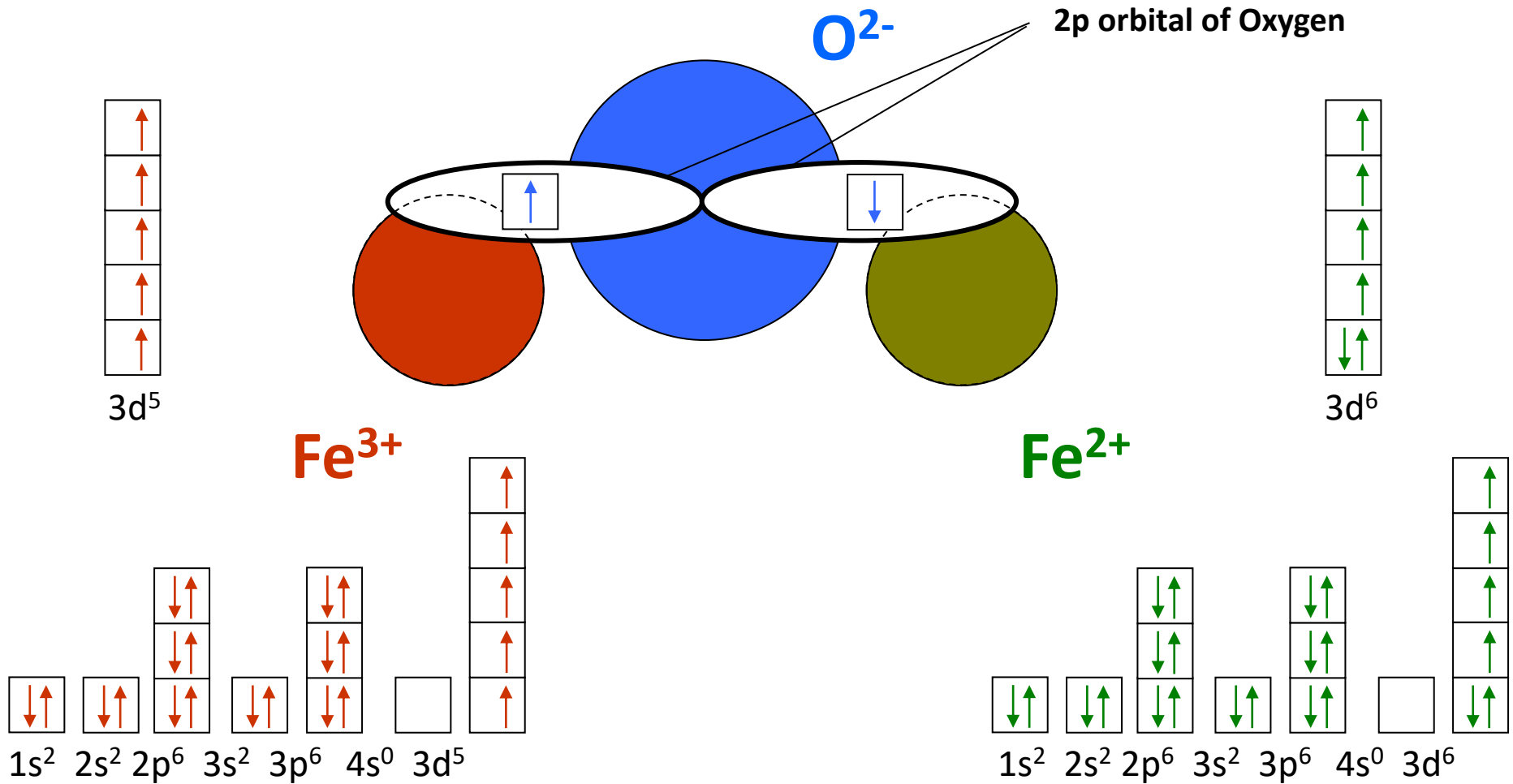


Close packing of oxygen & iron

# Superexchange

## Magnetite $\text{Fe}^{3+}[\text{Fe}^{3+}\text{Fe}^{2+}]\text{O}_4$

Oxygen 2p orbital overlaps with both 3d orbitals of  $\text{Fe}^{3+}$  and  $\text{Fe}^{2+}$

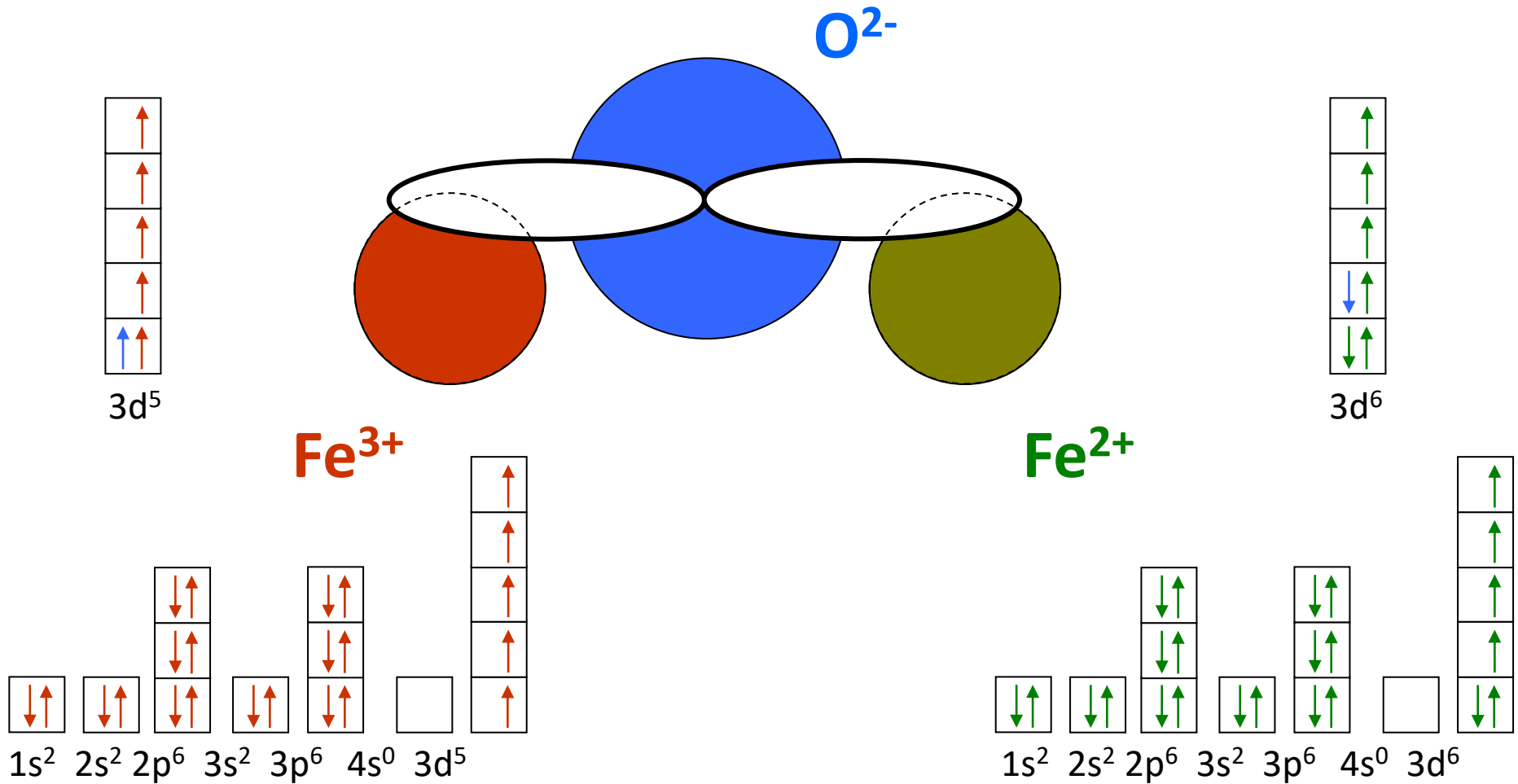




# Superexchange

Magnetite  $\text{Fe}^{3+}[\text{Fe}^{3+}\text{Fe}^{2+}]\text{O}_4$

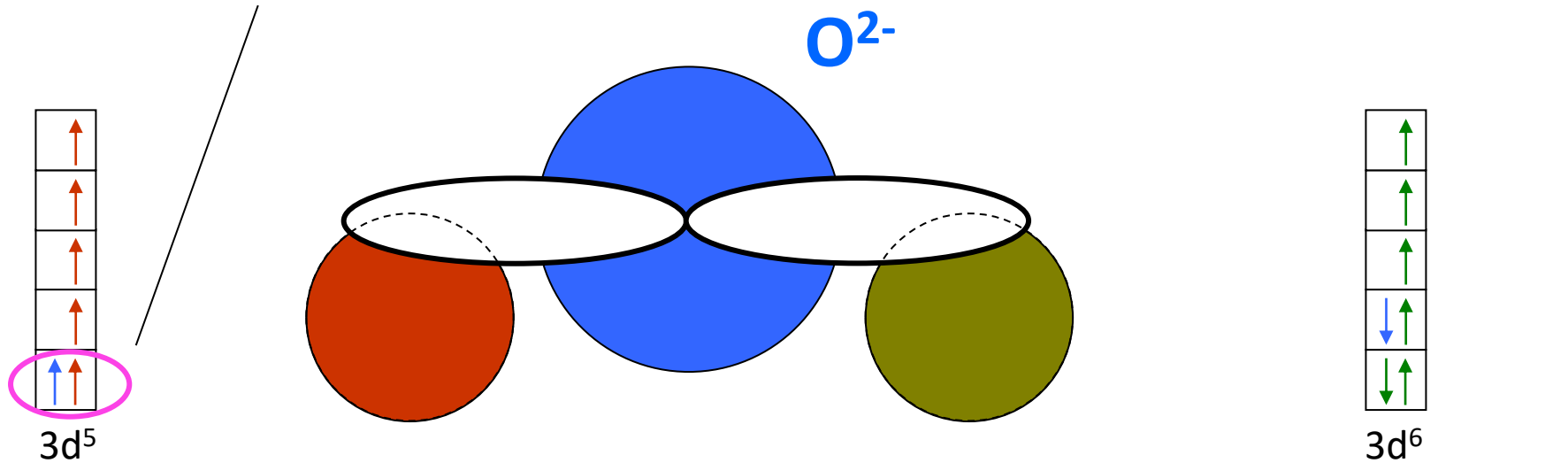
Oxygen exchanges both outer 2p electrons with the iron ions



# Superexchange

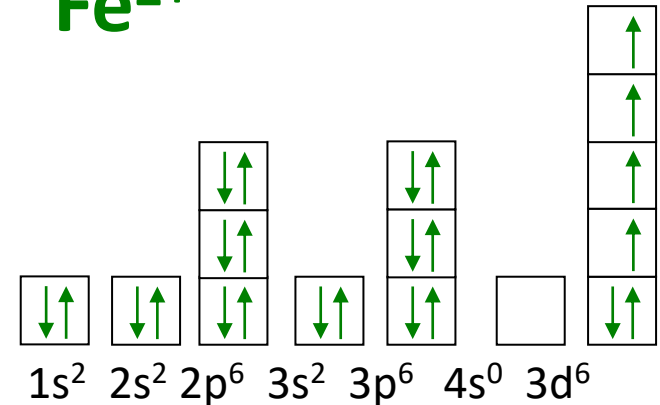
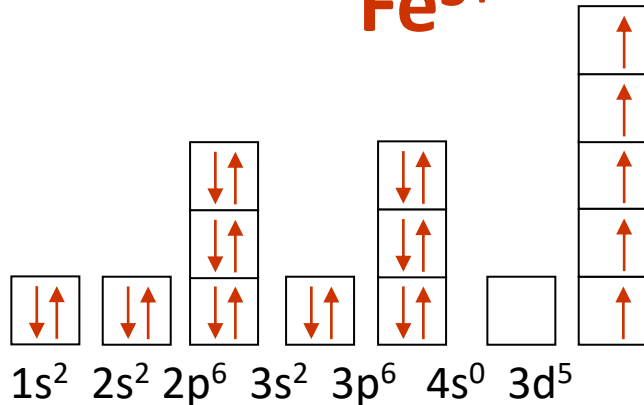
Magnetite  $\text{Fe}^{3+}[\text{Fe}^{3+}\text{Fe}^{2+}]\text{O}_4$

2 parallel spins  $\rightarrow$  violation of Pauli principle



$\text{Fe}^{3+}$

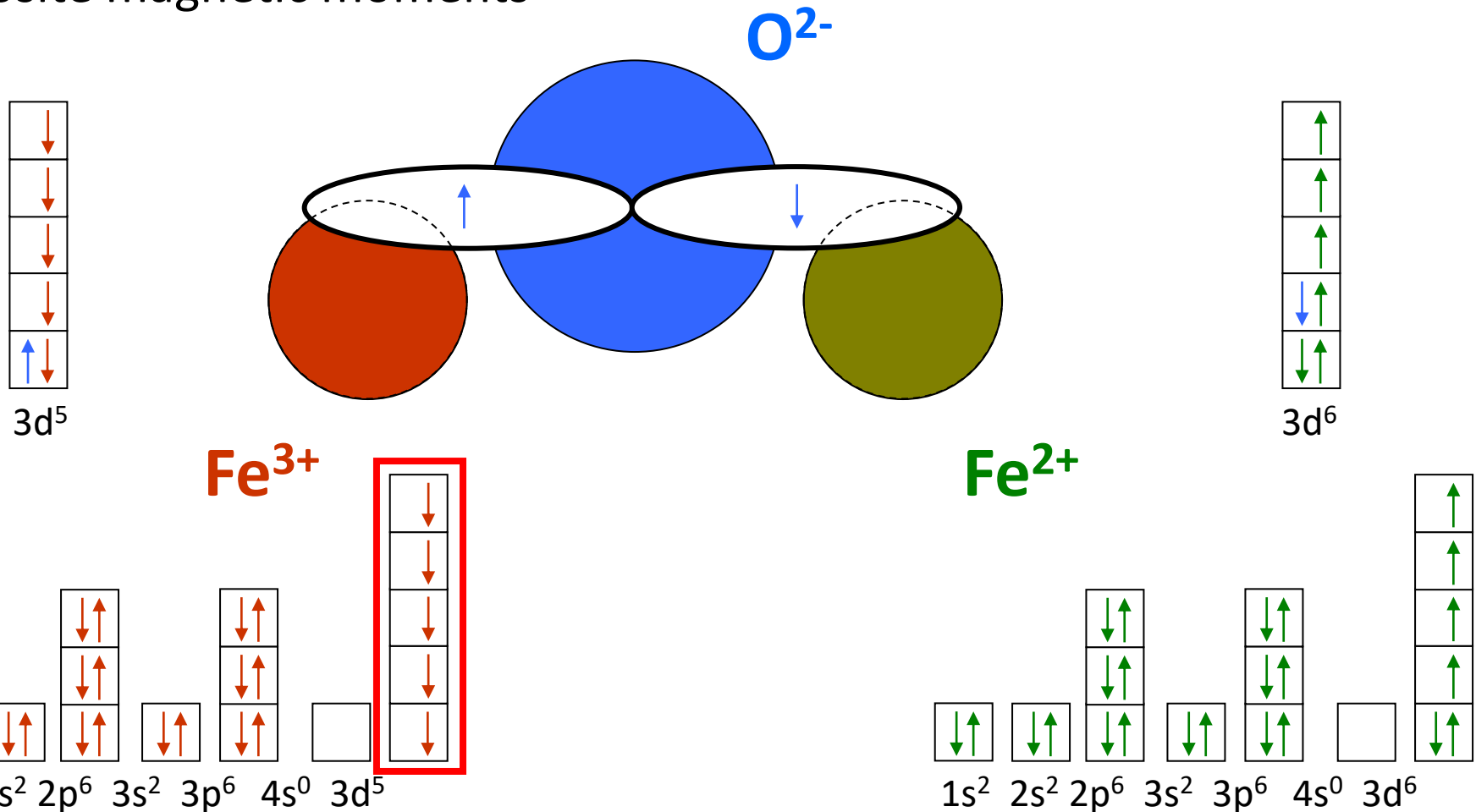
$\text{Fe}^{2+}$






# Superexchange

## Magnetite $\text{Fe}^{3+}[\text{Fe}^{3+}\text{Fe}^{2+}]\text{O}_4$

Solution: opposite spins of Fe-ions  $\rightarrow$  lattices with opposite magnetic moments



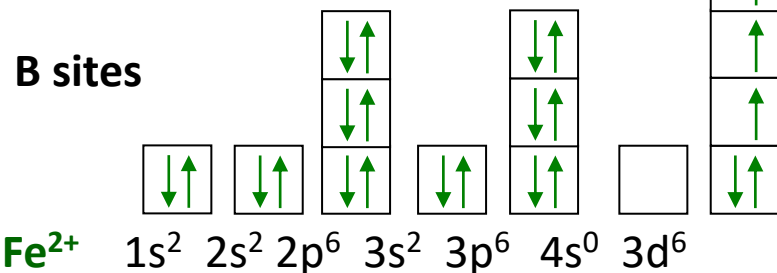
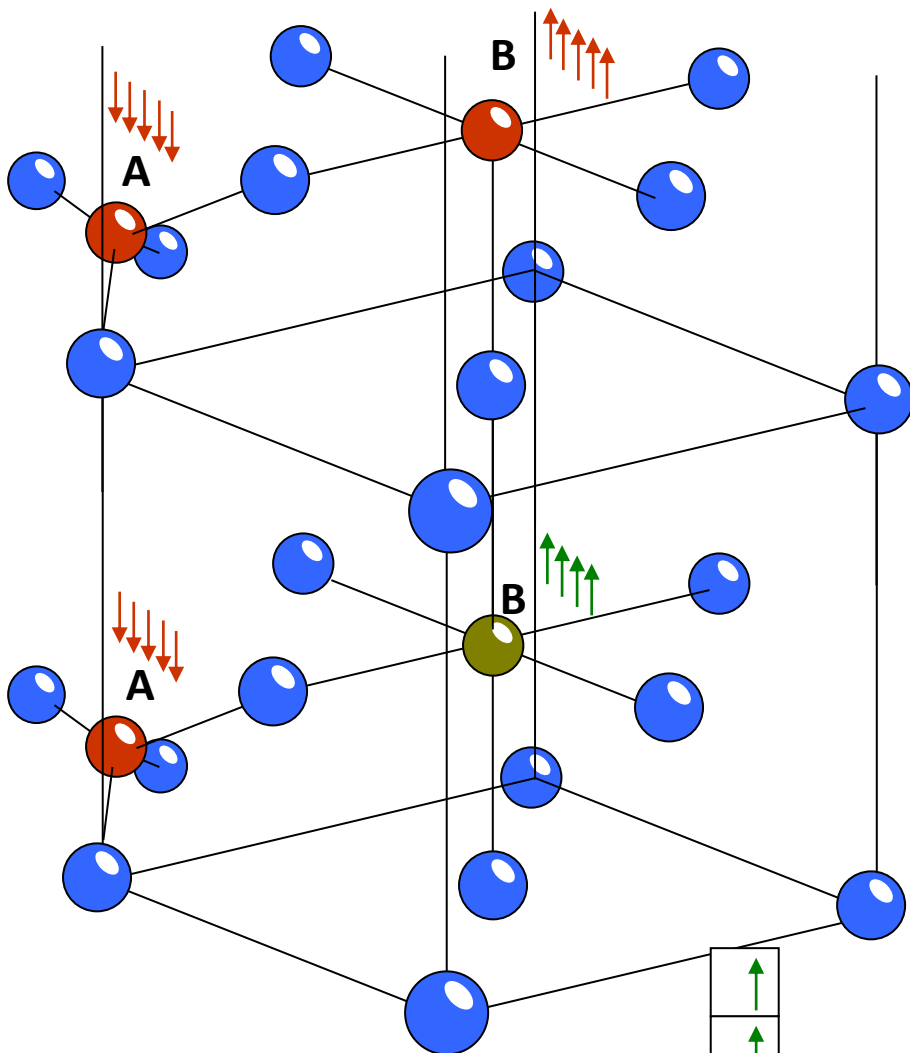
## Magnetite $\text{Fe}^{3+}[\text{Fe}^{3+}\text{Fe}^{2+}]\text{O}_4$

-  ferric iron  $\text{Fe}^{3+}$  at tetrahedral (A) and octahedral (B) sites
-  ferrous iron  $\text{Fe}^{2+}$  at octahedral site
-  oxygen anions




at tetrahedral sites,  $\text{Fe}^{3+}$  occurs only  
 at octahedral sites occur both,  $\text{Fe}^{3+}$  and  $\text{Fe}^{2+}$   
 whole crystal: spins of  $\text{Fe}^{3+}$  at A sites equal  
 spins of  $\text{Fe}^{3+}$  at B sites  $\rightarrow$  resulting moment  
 only from  $\text{Fe}^{2+}$   
 magnetic moments at A and B sites are  
 unequal and antiparallel  $\rightarrow$  ferrimagnetism

$$4 \mu_B$$

4 uncompensated moments



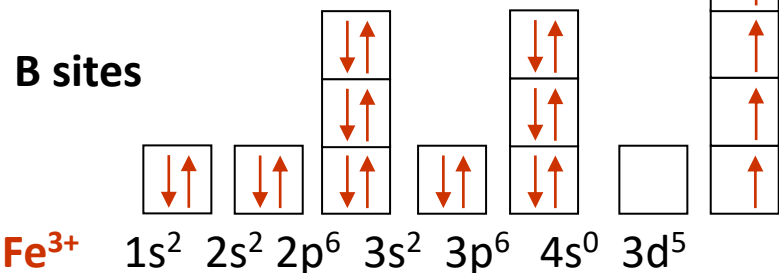
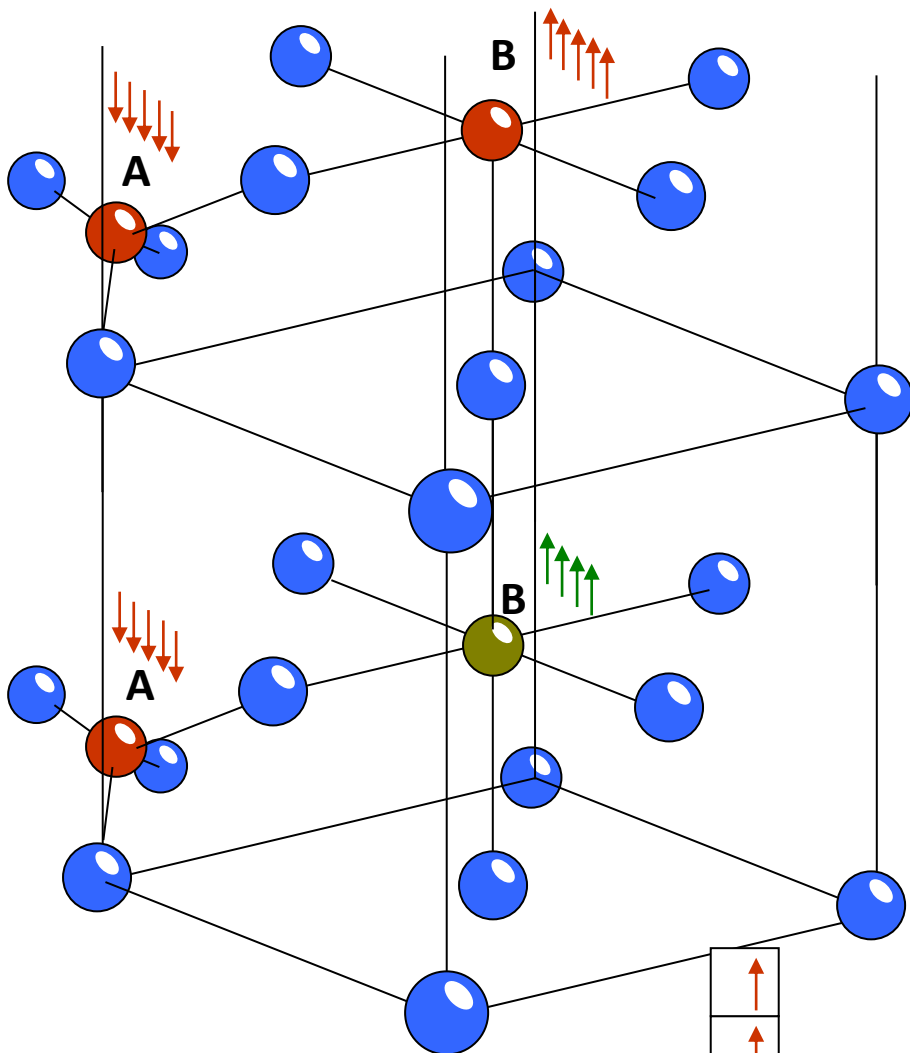
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$$4 \mu_B$$

**5** uncompensated moments



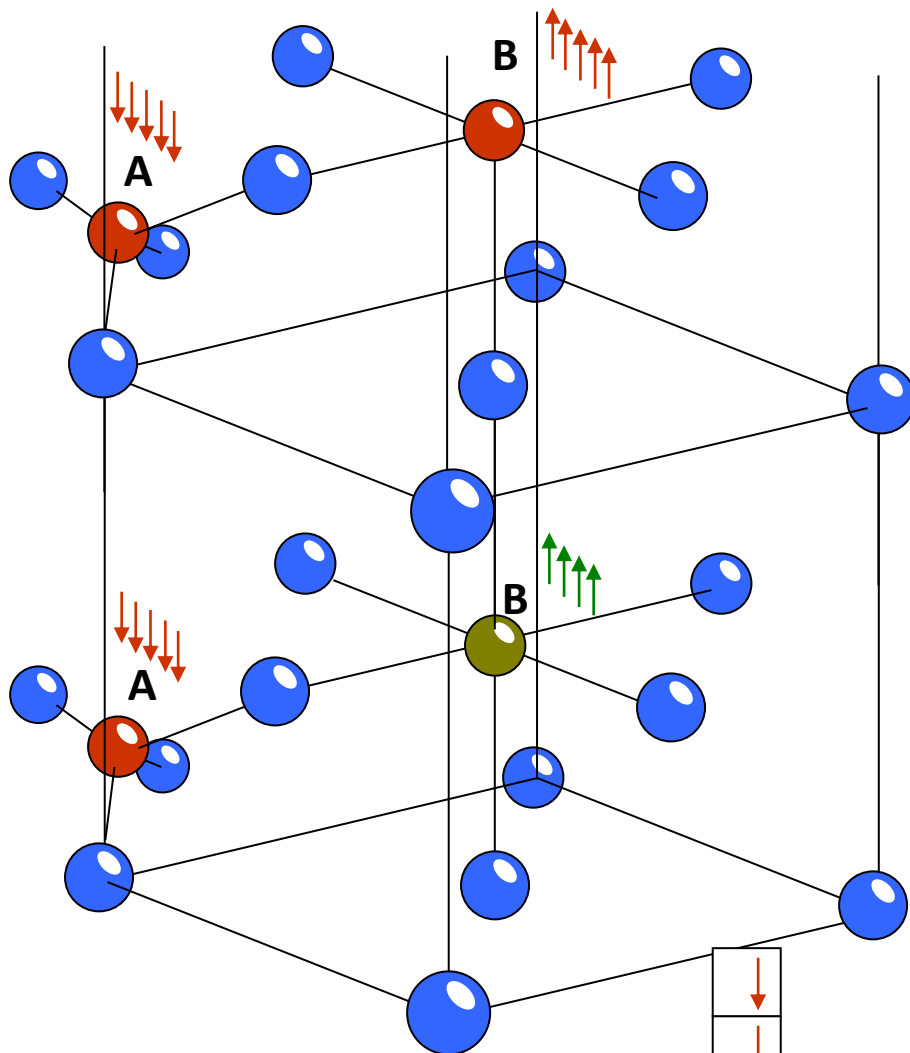
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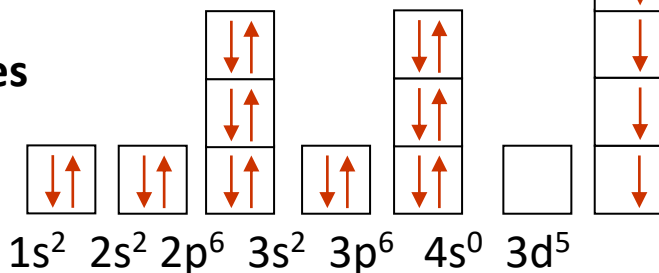
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**5** uncompensated moments

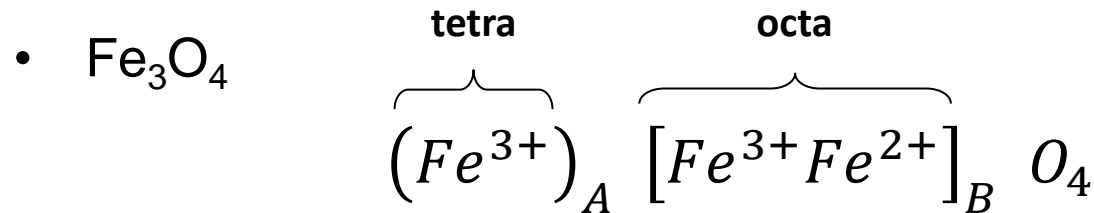


**A sites**

**$\text{Fe}^{3+}$**



## Magnetite



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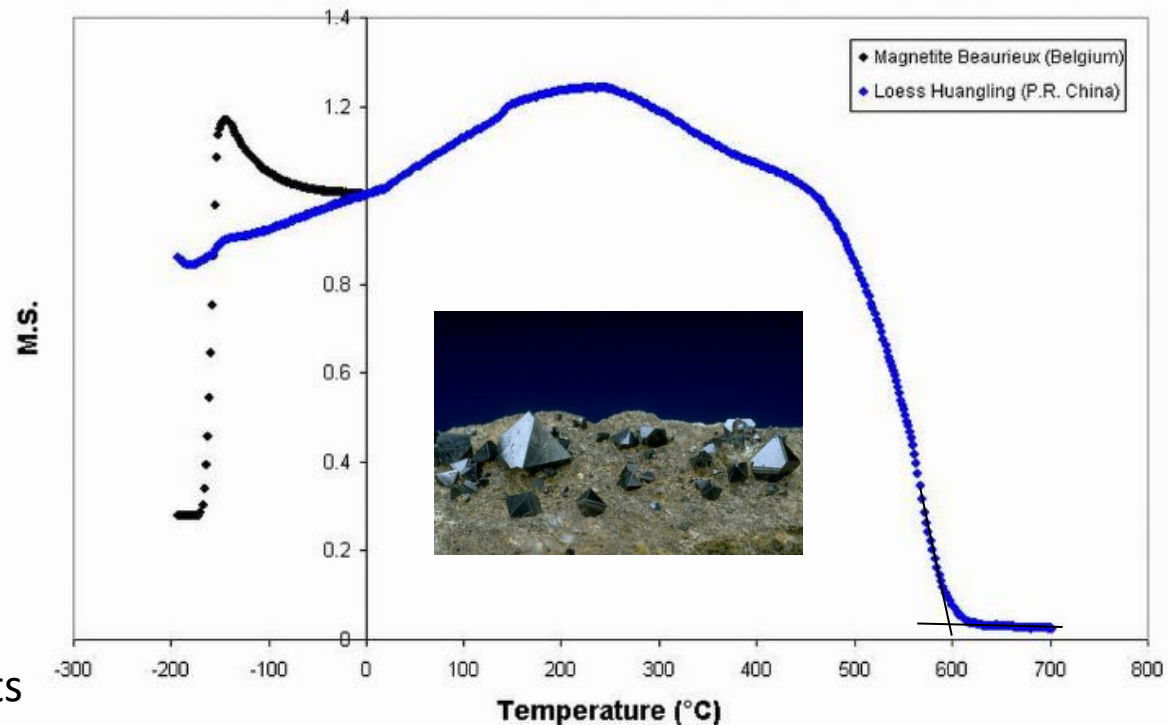
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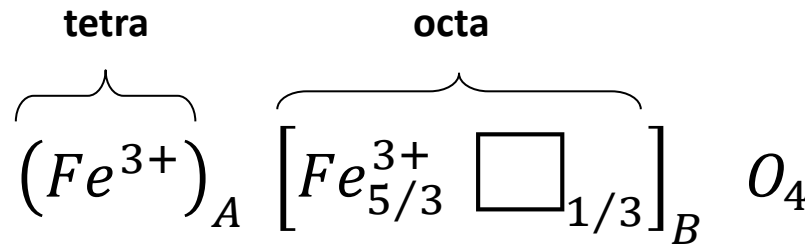
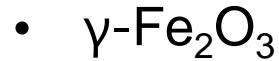
- (Soils)
- Inside bacteria
- Baked clays
- Combustion product
- Lacustrine/marine sediments

loss of magnetic ordering  
due to high thermal energy

characteristic temperature for  
each mineral  
but depends on substitution  
degree



## Maghaemite



$3.33 \mu_B$

**ferrimagnetic**

Oxidised magnetite

$M_S = 380 \text{ kA/m}$

$T_C = 645 \text{ }^\circ\text{C}$  (depends on substitution)

$T_V =$  depending on oxidation degree

Metastable 250 – 750 °C

Converts to haematite

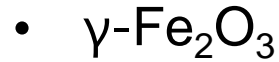
- Soils
- Soil bacteria excretion
- Baked clays
- Lacustrine/marine sediments



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## Maghaemite



Oxidation of 44 nm magnetite

at 30° and variable  $p_{\text{O}_2}$

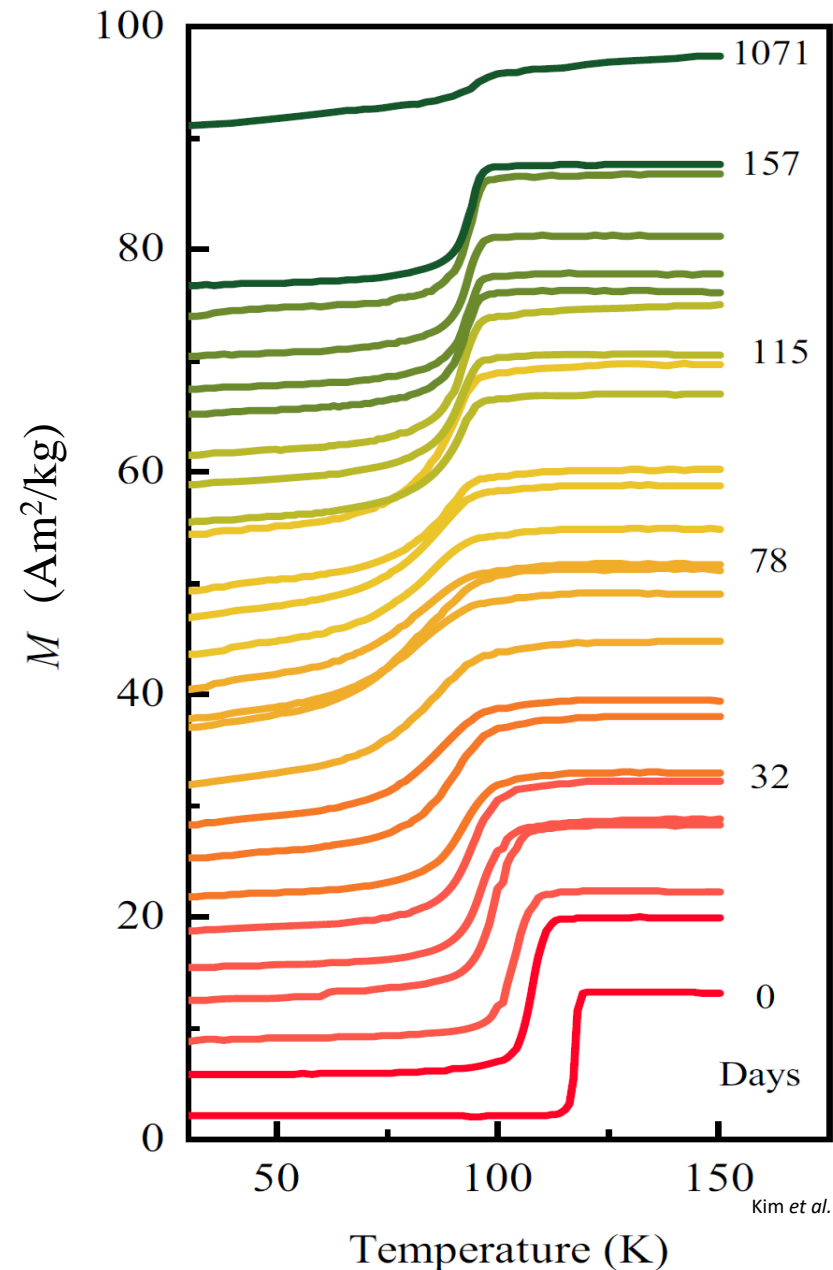
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Metastable 250 – 750 °C  
Converts to haematite

- Soils
- Soil bacteria excretion
- Baked clays
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Kim et al. 2021

## Haematite

- $\alpha\text{-Fe}_2\text{O}_3$

**"antiferromagnetic"**

$$M_S = 2.5 \text{ kA/m}$$

$$T_N = 680 - 690 \text{ }^\circ\text{C}$$

$$T_M = \text{between } -100 \text{ and } -13 \text{ }^\circ\text{C}$$

(size dependent)

$$H_c \text{ size dependent}$$

- Soils
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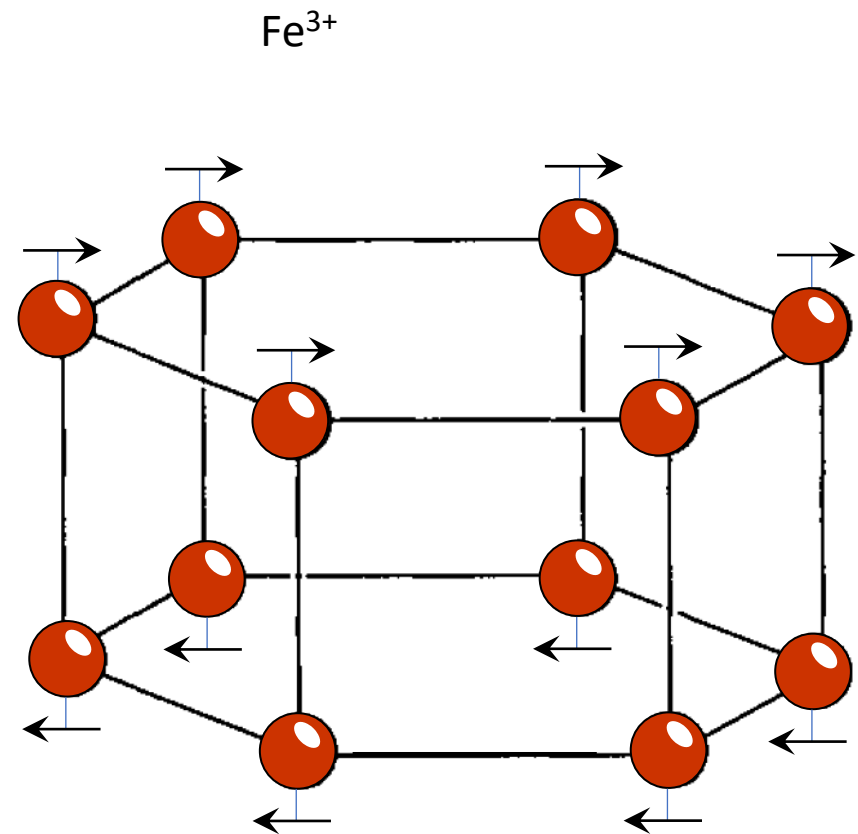
(size dependent)

$$H_c \text{ size dependent}$$

- Soils
- Baked clay
- Sediments



- apparent antiparallel alignment of spins



Modified from Evans & Heller 2003

## Haematite

- $\alpha\text{-Fe}_2\text{O}_3$

- Imperfect antiparallel alignment of spins

$$M_S = 2.5 \text{ kA/m}$$

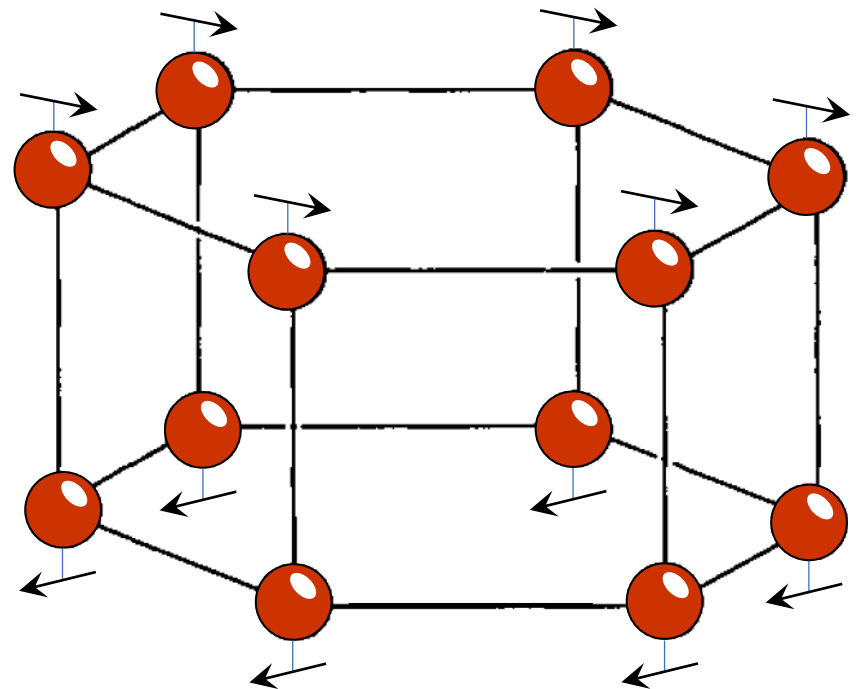
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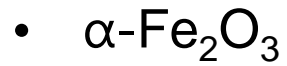
$$H_c \text{ size dependent}$$

- Soils
- Baked clay
- Sediments



Modified from Evans & Heller 2003

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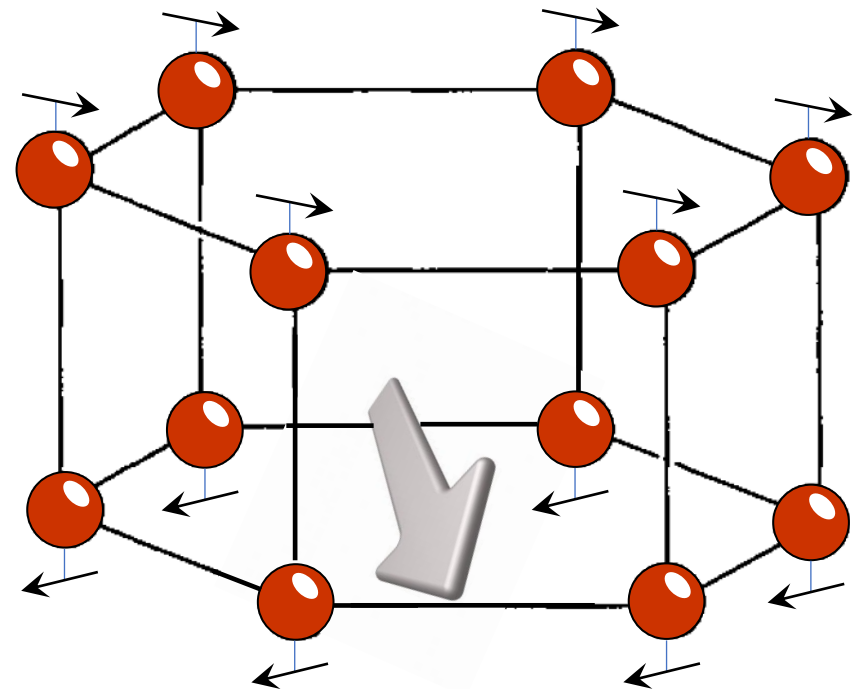
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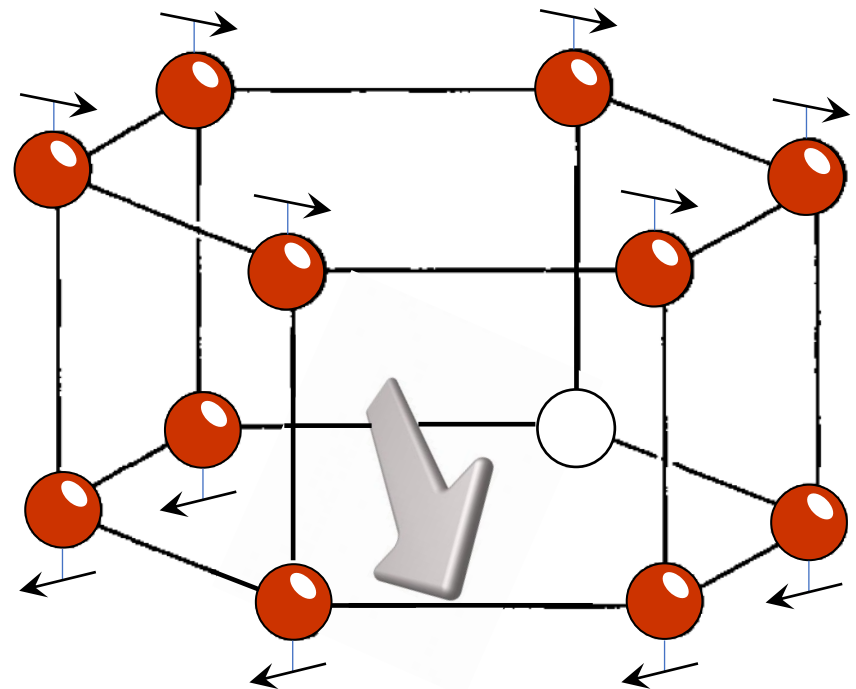
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- Soils
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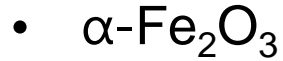
- Imperfect antiparallel alignment of spins
- Holes in crystal lattice (defects)

→ weakly ferromagnetic behaviour



Modified from Evans & Heller 2003

## Haematite



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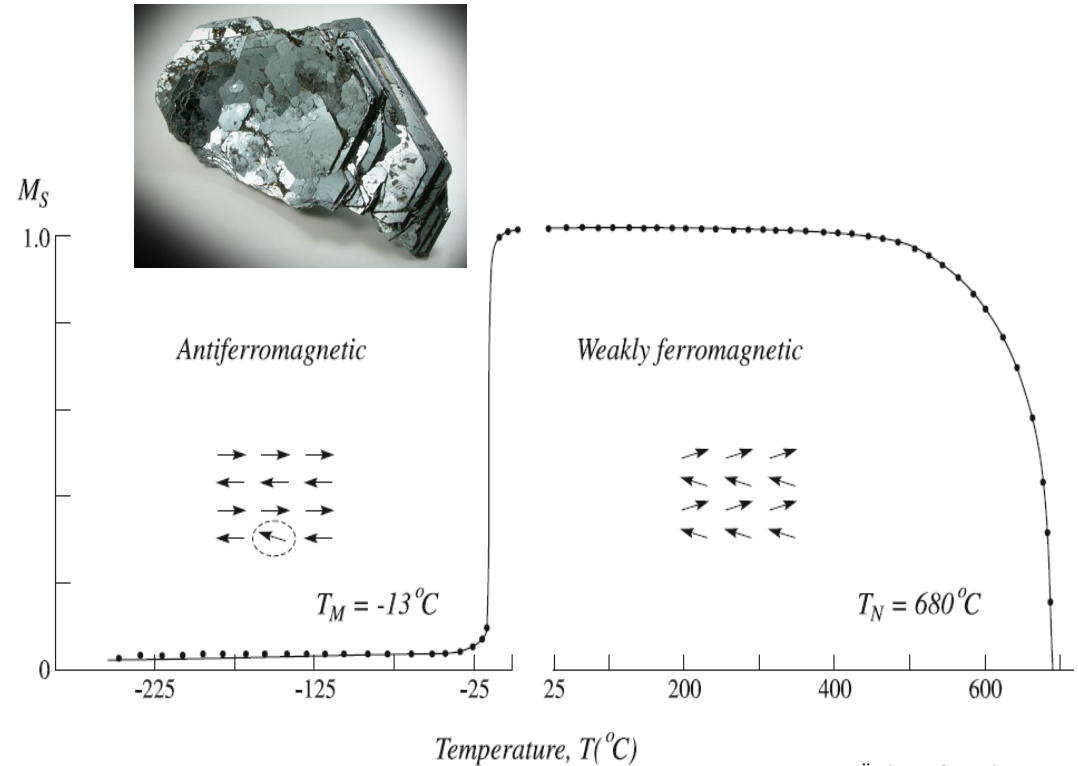
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→ weakly ferromagnetic behaviour



Özdemir & Dunlop 2006

## Haematite

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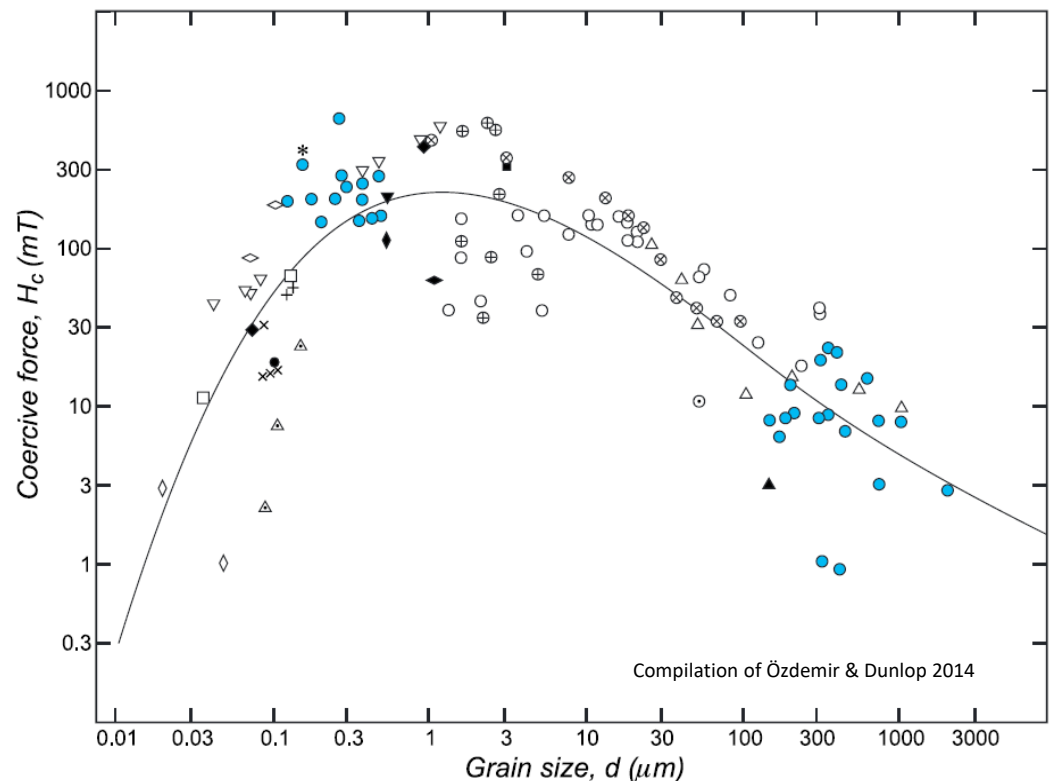
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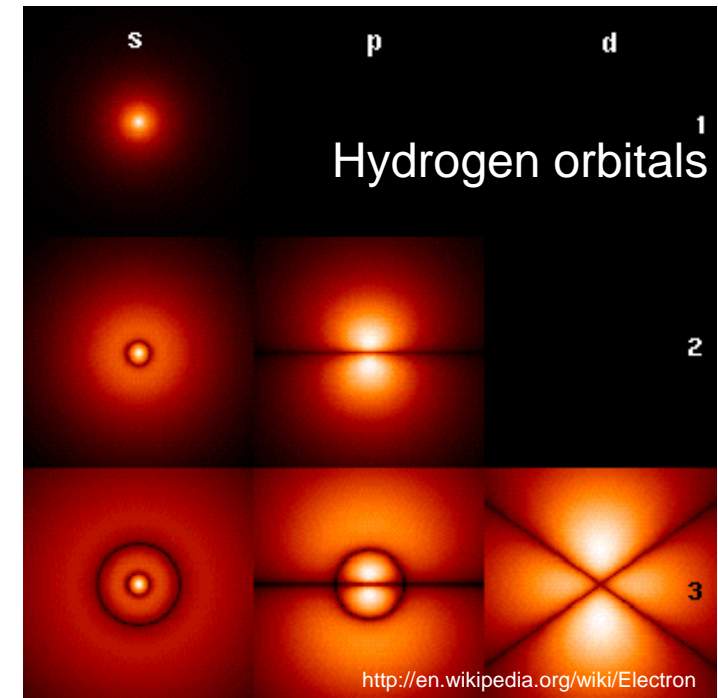
→ weakly ferromagnetic behaviour





## Origin of magnetism

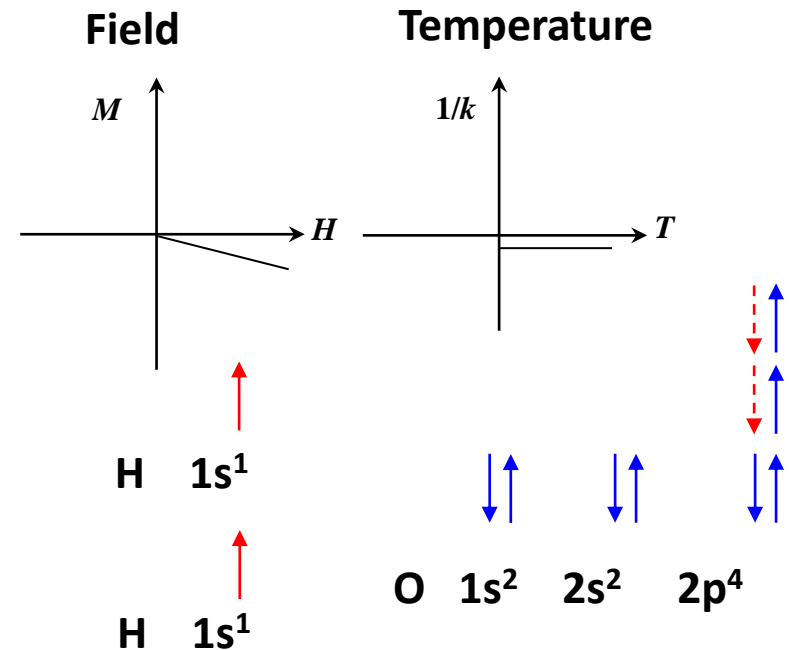
- Electrons carry a spin magnetic moment
- In crystals with uncompensated spins
- Ordering requires energy gain by spin coordination of electrons in overlapping orbitals.
- Only ions with uncompensated spins in highly eccentric orbitals (e.g. 3d for  $Fe^{3+}$ ) are possible sources of ferro-, ferri- or antiferromagnetism.



## Diamagnetism ( $\kappa < 0$ )

- external magnetic field  $H$  causes distortion of electron-orbit (*Lorentz force*)
- precession of orbital plane around  $H$  direction (*Larmor-precession*)
- a second magnetic moment is created but opposite to  $H$  (*Lenz rule*)
- precession frequency depends on  $H$
- in all materials
- weak, best observed in materials without a resulting spin momentum

Calcite	$\text{CaCO}_3$	$- 0.48 \times 10^{-8} \text{ m}^3/\text{kg}$
Quartz	$\text{SiO}_2$	$- 0.62 \times 10^{-8} \text{ m}^3/\text{kg}$
Water	$\text{H}_2\text{O}$	$- 0.90 \times 10^{-8} \text{ m}^3/\text{kg}$



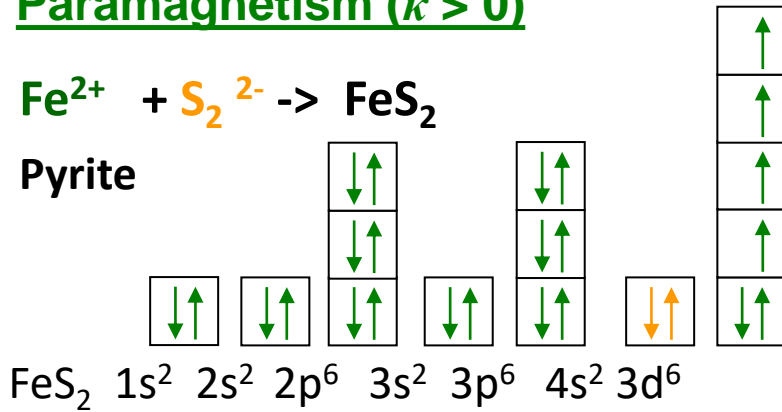
# Summary

# Magnetic minerals

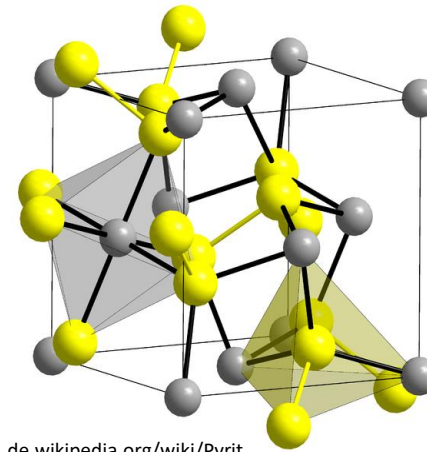
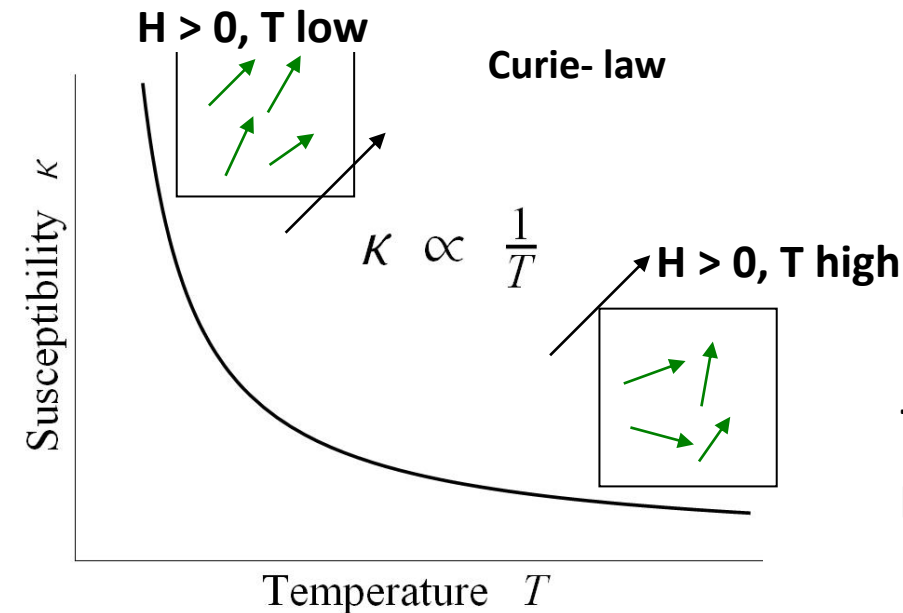
## Paramagnetism ( $\kappa > 0$ )



Pyrite



4 uncompensated moments



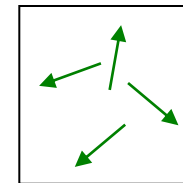
de.wikipedia.org/wiki/Pyrit



de.wikipedia.org/wiki/Kubisches\_Kristallsystem

non-overlapping atomic orbitals

$H = 0$

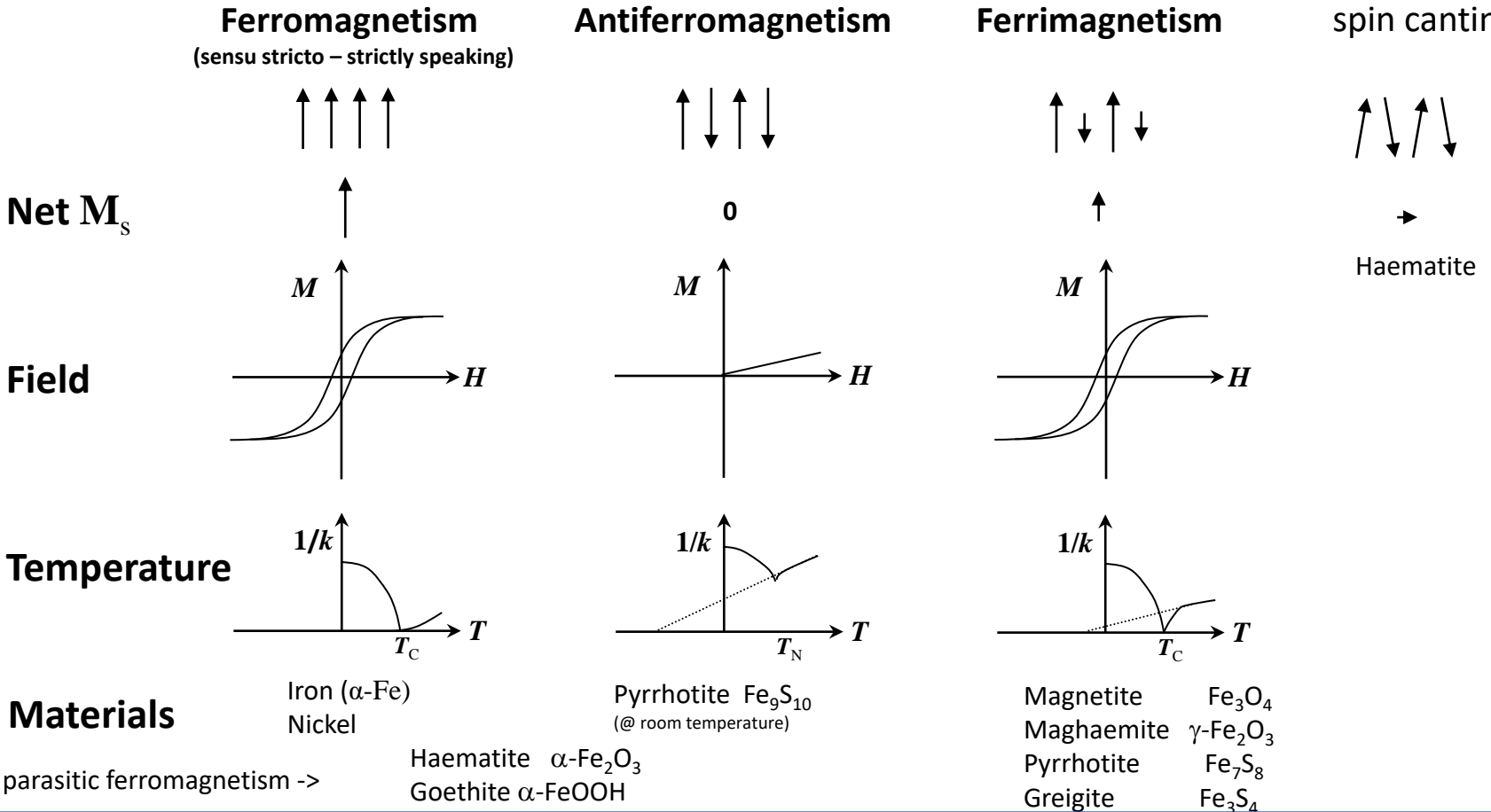


random spin alignment

thermal energy randomises spin alignment  
hence spin alignment depends on temperature

## Ferromagnetism ( $\kappa \gg 0$ )

- in materials with unpaired spins and overlapping atom orbits (close packing)
- electrons are exchanged between iron atoms either directly (ferromagnetism) or indirectly via interjacent oxygen atoms (superexchange – e.g. antiferromagnetism, ferrimagnetism)
- materials exhibit a spontaneous magnetisation  $M_s$  after field removal, due to uncompensated spin moments



- Magnetite ( $\text{Fe}_3\text{O}_4$ ):**  $M_s = 480 \text{ kA/m}$ ,  $T_c = 580 \text{ }^\circ\text{C}$ ,  $T_v = -150 \text{ }^\circ\text{C}$   
ferrimagnetic, in soils, bacteria, lacustrine/marine sediments, often partly oxidised, also in human and animal tissue, combustion product
- Maghaemite ( $\gamma\text{-Fe}_2\text{O}_3$ ):**  $M_s = 380 \text{ kA/m}$ , ( $T_c = 590\text{-}675 \text{ }^\circ\text{C}$ )  
ferrimagnetic weathering product (fully oxidised magnetite, no  $\text{Fe}^{2+}$  in lattice), common in soils and sedimentary rocks, combustion product
- Haematite ( $\alpha\text{-Fe}_2\text{O}_3$ ):**  $M_s = \sim 2.5 \text{ kA/m}$ ,  $T_c = 675 \text{ }^\circ\text{C}$ ,  $T_M = -15 \text{ }^\circ\text{C}$ ,  
imperfect antiferromagnet (weakly ferromagnetic) common in soils and sediments, red beds
- Pyrrhotite ( $\text{Fe}_7\text{S}_8$ ):**  $M_s = \sim 80 \text{ kA/m}$ ,  $T_c = 320 \text{ }^\circ\text{C}$
- Pyrrhotite ( $\text{Fe}_9\text{S}_{10}$ ):** ferrimagnetic above  $200 \text{ }^\circ\text{C}$ ,  $T_c = 265 \text{ }^\circ\text{C}$   
in sedimentary metamorphic rocks, sulfide ores
- Greigite ( $\text{Fe}_3\text{S}_4$ ):**  $M_s = \sim 125 \text{ kA/m}$ ,  $T_c = \sim 330 \text{ }^\circ\text{C}$   
forms in aquatic environments (and soils) under unoxic conditions, in bacteria
- Goethite ( $\alpha\text{-FeOOH}$ ):**  $M_s = \sim 2 \text{ kA/m}$ ,  $T_c = 120 \text{ }^\circ\text{C}$   
imperfect antiferromagnet (weakly ferromagnetic), in soils and aquatic environments, lateritic weathering product
- Siderite ( $\text{FeCO}_3$ ):**  $T_N = -235 \text{ }^\circ\text{C}$  (antiferromagnetic, but paramagnetic @ room temperature) marine lacustrine, in soils probably

- *Properties of some magnetic minerals*
- *Formation of magnetic minerals*
- *Magnetic characterisation methods*
- *Examples*

## Soils

Dead vegetable and animal matter is decomposed by soil animals and microorganisms (such as worms, mollusca, bacteria, fungi), altered and incorporated into the soil. -> humification of organic matter.

Source material and products of weathering/humification are transported on and in the soil, either as solid particles or in solutions.

The soil constituents are then connected by cementing material, which is partly of biologic origin. This causes a new texture and granularity.

**Woodlouses** (Armadillidium)



**Mites**

(Acari)



**Fungi**



**Earthworms**

Pedogenesis = progressive transformation of bed rock into a soil

Bed rock subjected to

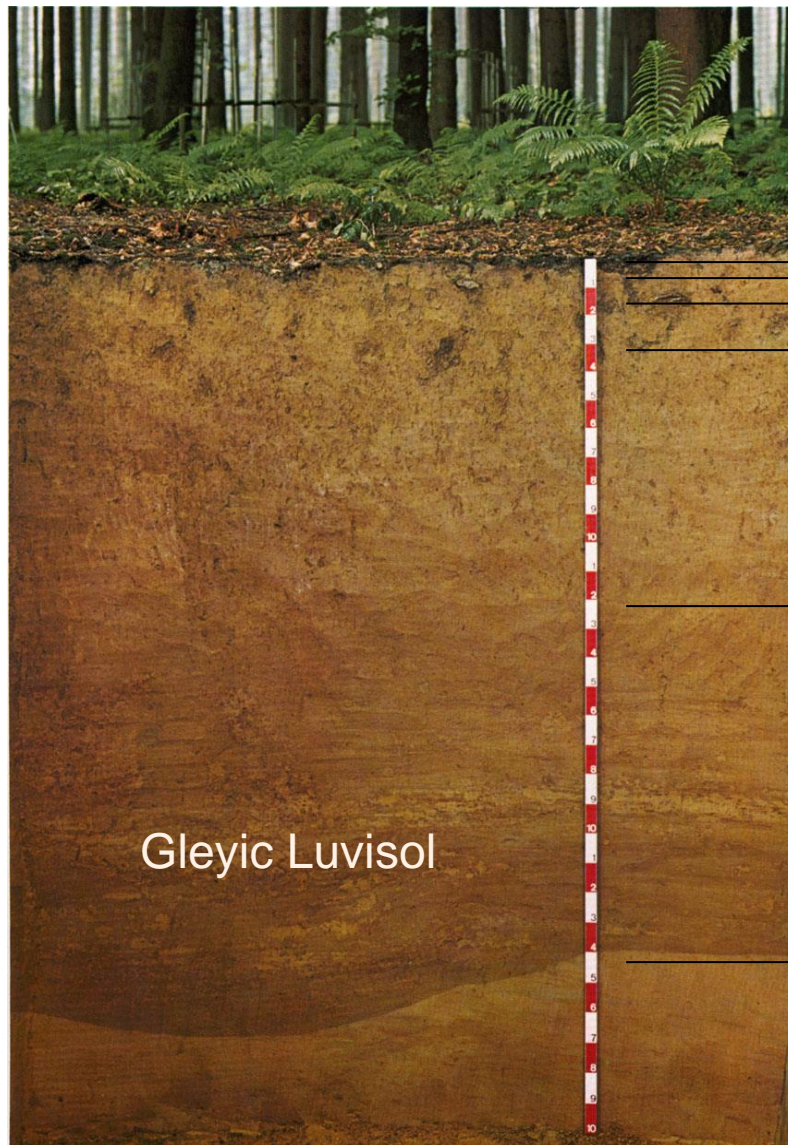
Physical processes

- temperature differences
- dilatation shrinking

Chemical processes

- hydrolysis,
- dissolution,
- oxidation, hydration/dehydration

**Ionic iron supply  
from bedrock**



O – organic horizon (organic matter)

A<sub>h</sub> – mineral horizon (humified organic matter)

E – eluvial horizon (with lighter colour)

B<sub>tg</sub> – argillic horizon, partly gleyic

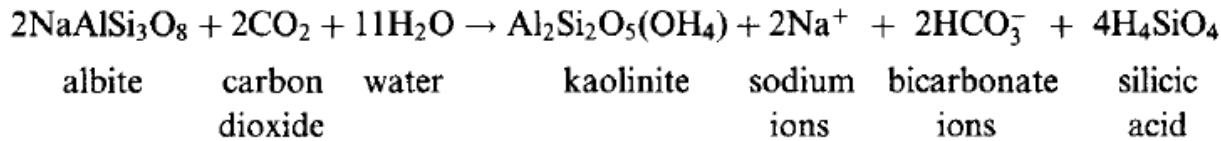
B<sub>g</sub> – horizon with manganese concretions

C – loess

Gleyic Luvisol

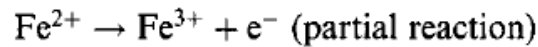


## I. Hydrolysis

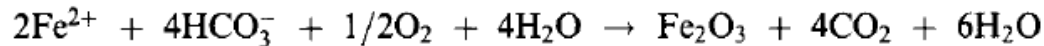


Destruction of silicates

## II. Oxidation



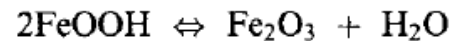
ferrous ion
ferric ion
electron to other element



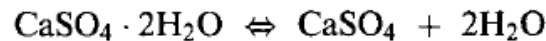
ferrous ions
bicarbonate ions
oxygen
water
hematite
carbon dioxide
water

Fe<sup>2+</sup> from pyroxene/olivine  
To Fe<sup>3+</sup> in hematite  
goethite

## III. Hydration and dehydration



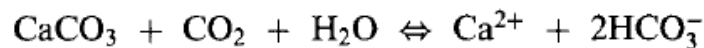
goethite
hematite
water



gypsum
anhydrite
water

Water bound/released in  
crystal lattice

## IV. Dissolution



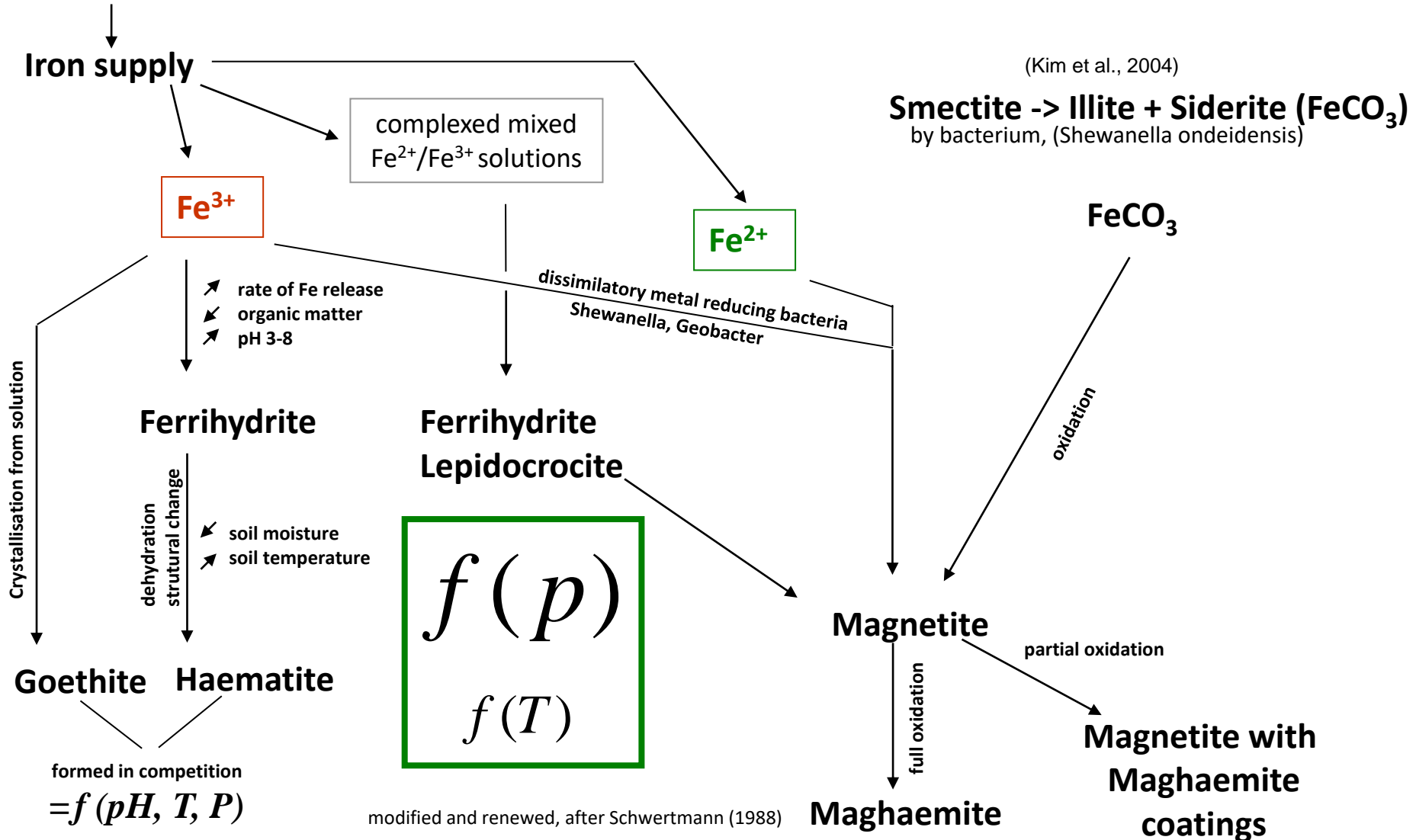
calcite
carbon dioxide
water
calcium ion
bicarbonate ions

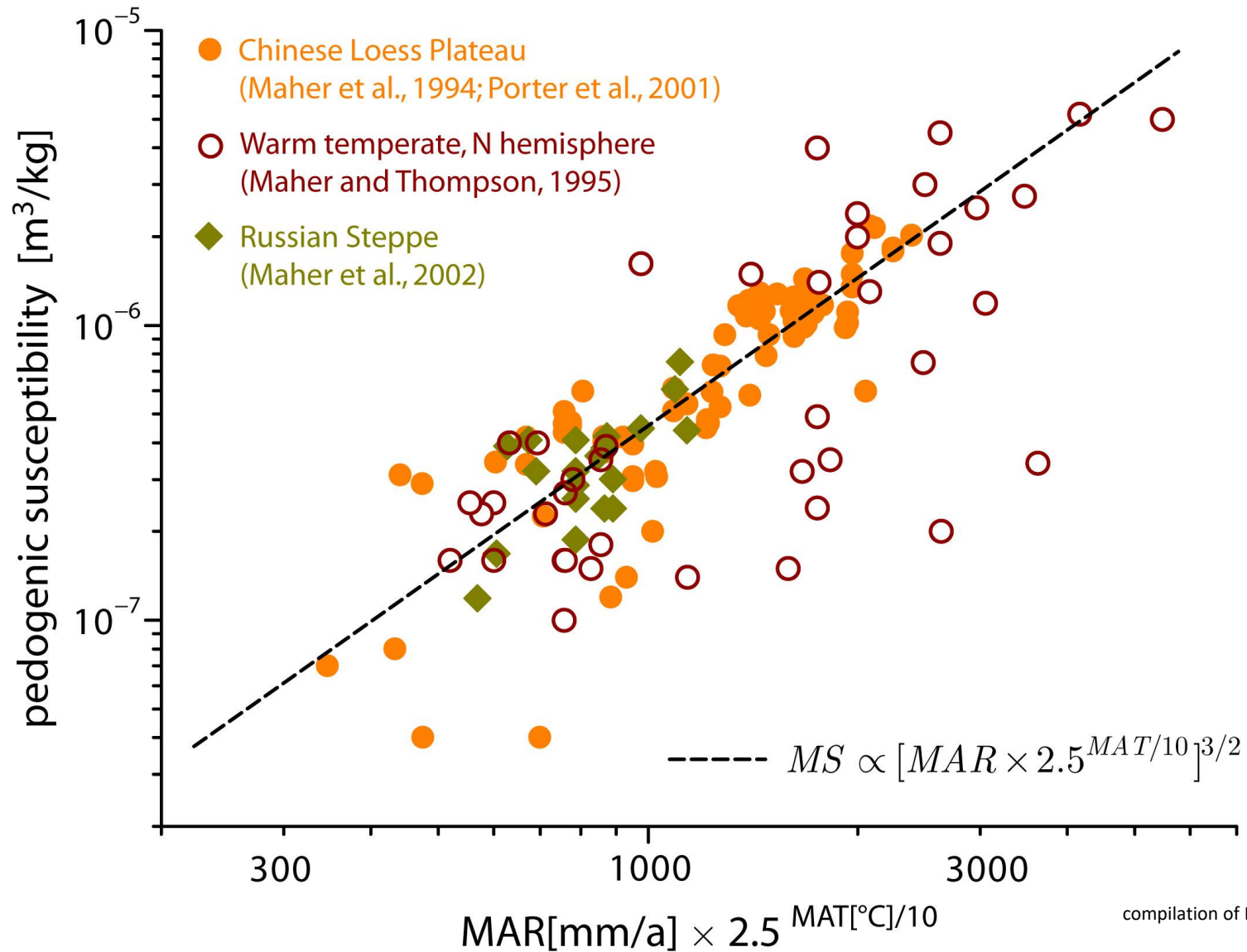
Carbonate dissolution and  
precipitation

From Garrels and Mackenzie, 1971; compiled by Retallack, 1990 (© Kluwer Academic Publishers, with kind permission of Kluwer Academic Publishers and the author).

## Soils

Chemical weathering of clay (e.g. smectite) and other ferrous silicates (e.g. fayalite)





compilation of Egli 2006



Roman pottery kiln at Bruyelle (Belgium)

## Baked materials

Source material contains “non”-magnetic iron

Magnetic minerals are generated during prolonged heat exposure at different  $p_{O_2}$



Muskovit



Phlogopit



Apophyllit



Talk



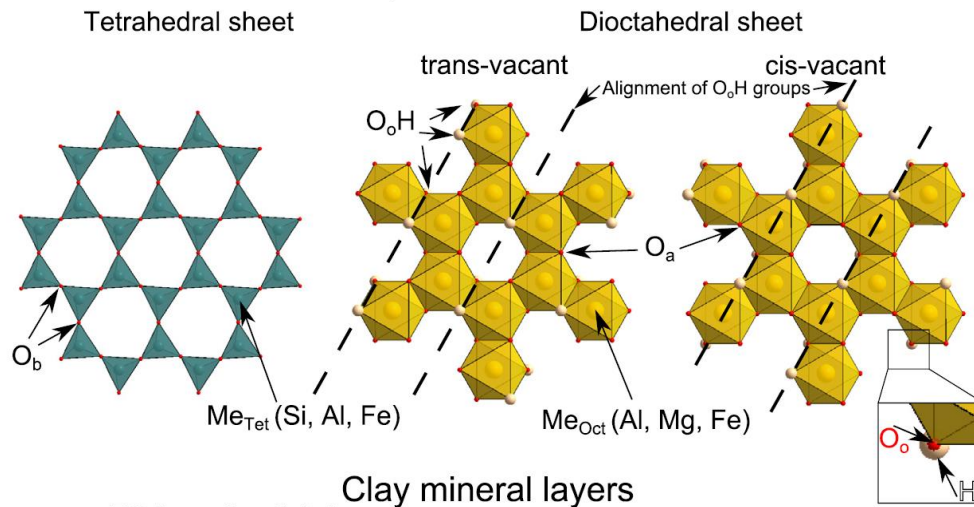
Carletonit

© de.wikipedia

## Phyllosilicates (e.g. clays, micas, chlorites) Murad & Wagner 1998

1. Loss of physically adsorbed or intercalated water at 100–200 °C
2. Oxidation, where applicable, of divalent iron
3. Loss of structural hydroxyl at intermediate higher temperatures
4. Final structural breakdown combined with the formation of new phases close to 1000 °C
5. Vitrification.

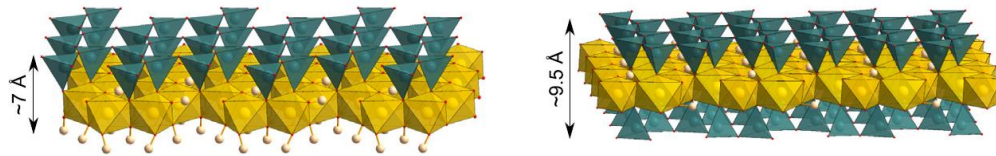
## Clay mineral sheets



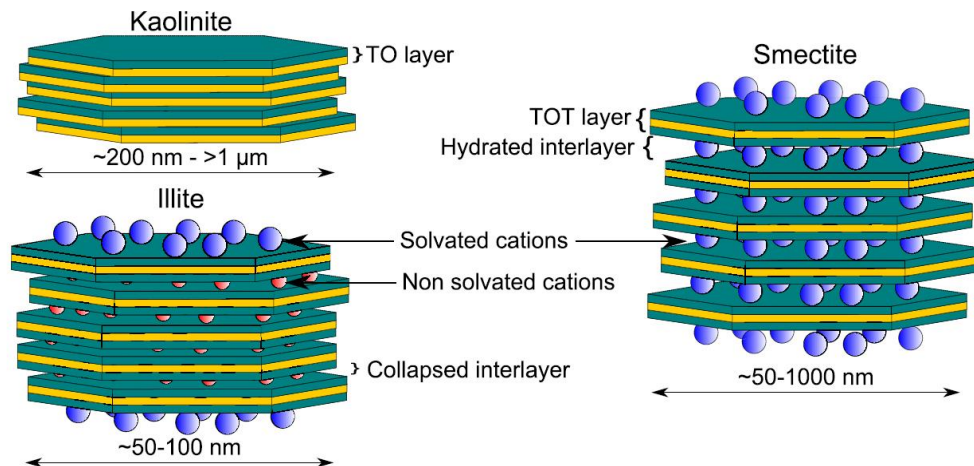
## Clay mineral layers

TO layer (kaolinite)

TOT layer (cv)



## Clay mineral particles



Tournassat *et al.* 2015

**FIGURE 1.1** From top to bottom: tetrahedral and octahedral sheets, TO (Kaol) and TOT layers (cv-Mt), and clay mineral particles. The Kaol layer structure was taken from the COD database (Gražulis *et al.*, 2012). The cv-Mt structure was taken from Tshipursky and Drits (1984).

## Baked materials

Source material contains “non”-magnetic iron

Magnetic minerals are generated during prolonged heat exposure at different  $p_{O_2}$

### Iron minerals

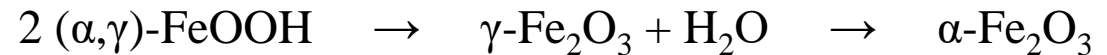
Murad & Wagner 1998 (and references therein)

#### Dehydroxylation under

200 - 320°C

310-485°C

**oxidising conditions**



**reducing conditions**

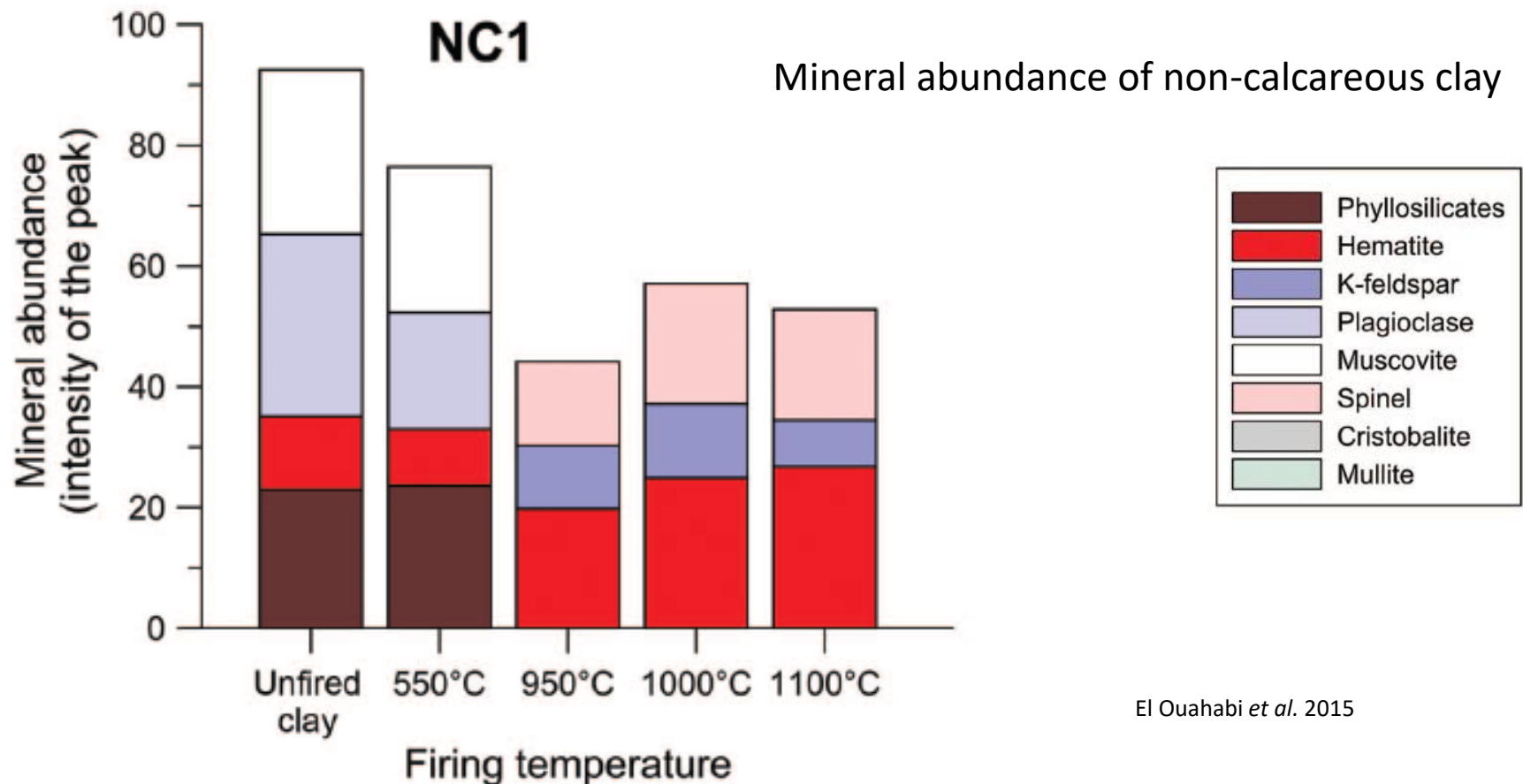


Presence of *Al* and *Ti* in clay can result in substituted maghaemite and haematite.

## Baked materials

Source material contains “non”-magnetic iron

Magnetic minerals are generated during prolonged heat exposure at different  $p_{O_2}$



El Ouahabi *et al.* 2015





Roman pottery kiln at Bruyelle (Belgium)

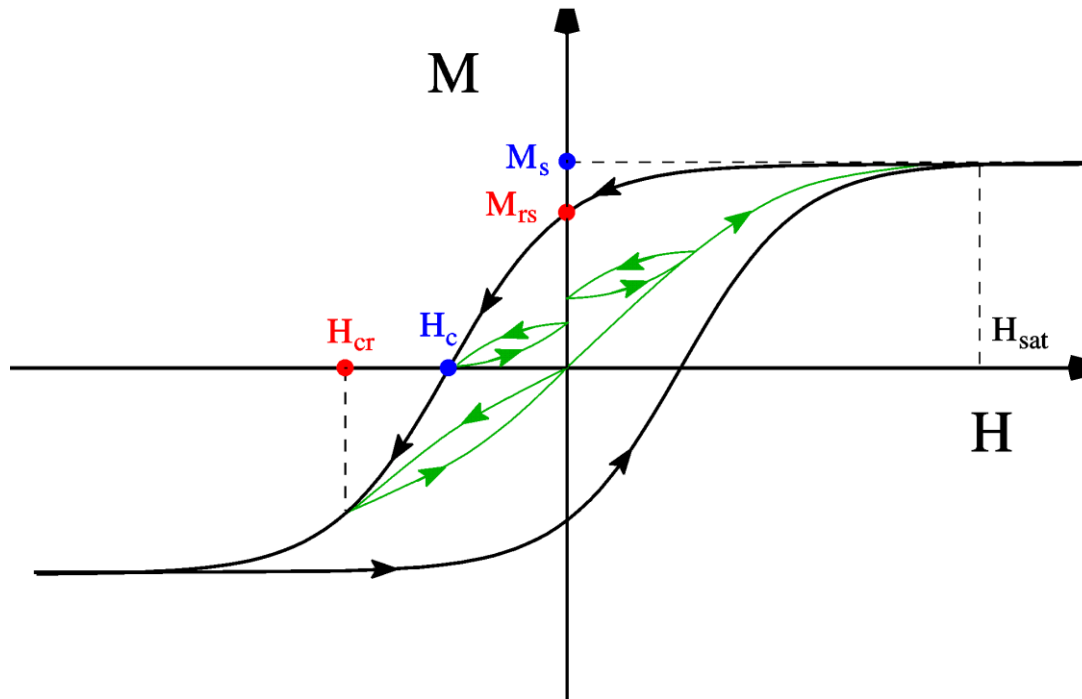
- *Properties of some magnetic minerals*
- *Formation of magnetic minerals*
- ***Magnetic characterisation methods***
- *Examples*

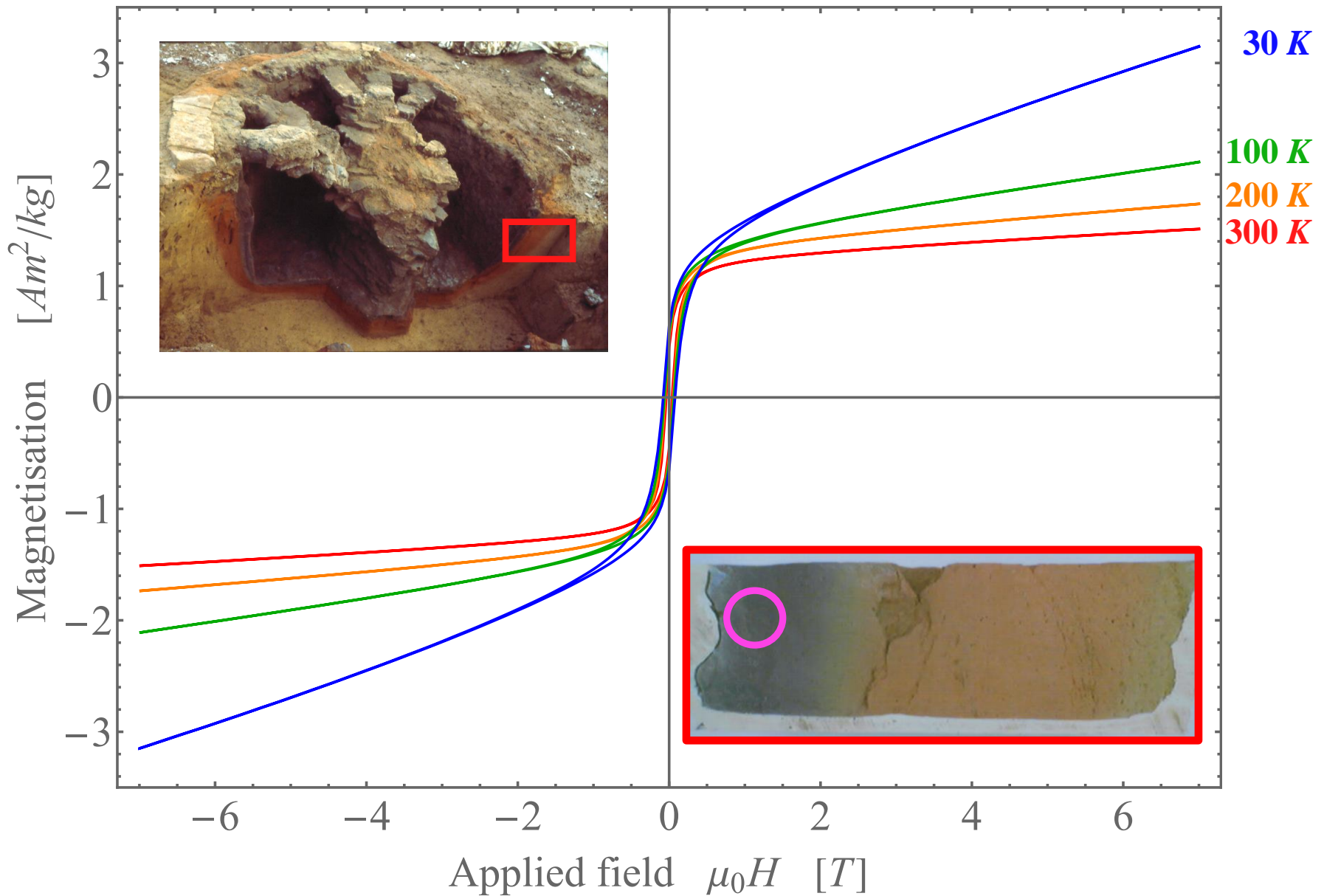
Loops RT LT, Day, exchange bias, Pasha,  
FORC nur am rande  
Coercivity spectra analysis nur am rande

## Magnetic hysteresis

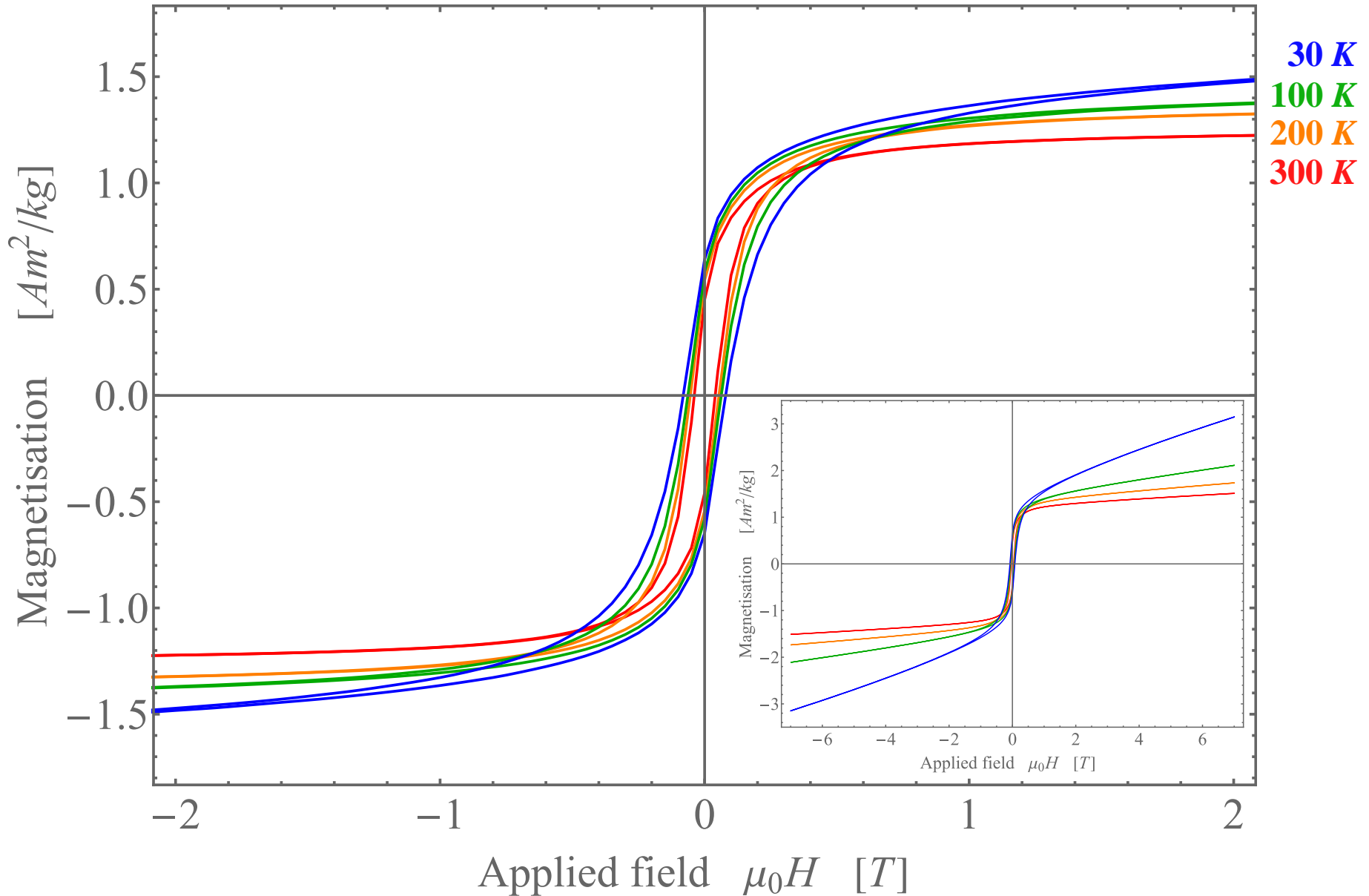
- $H_c$  – coercive force
- $H_{cr}$  – remanent coercive force
- $M_s$  – saturation magnetisation
- $M_{rs}$  – saturation remanence

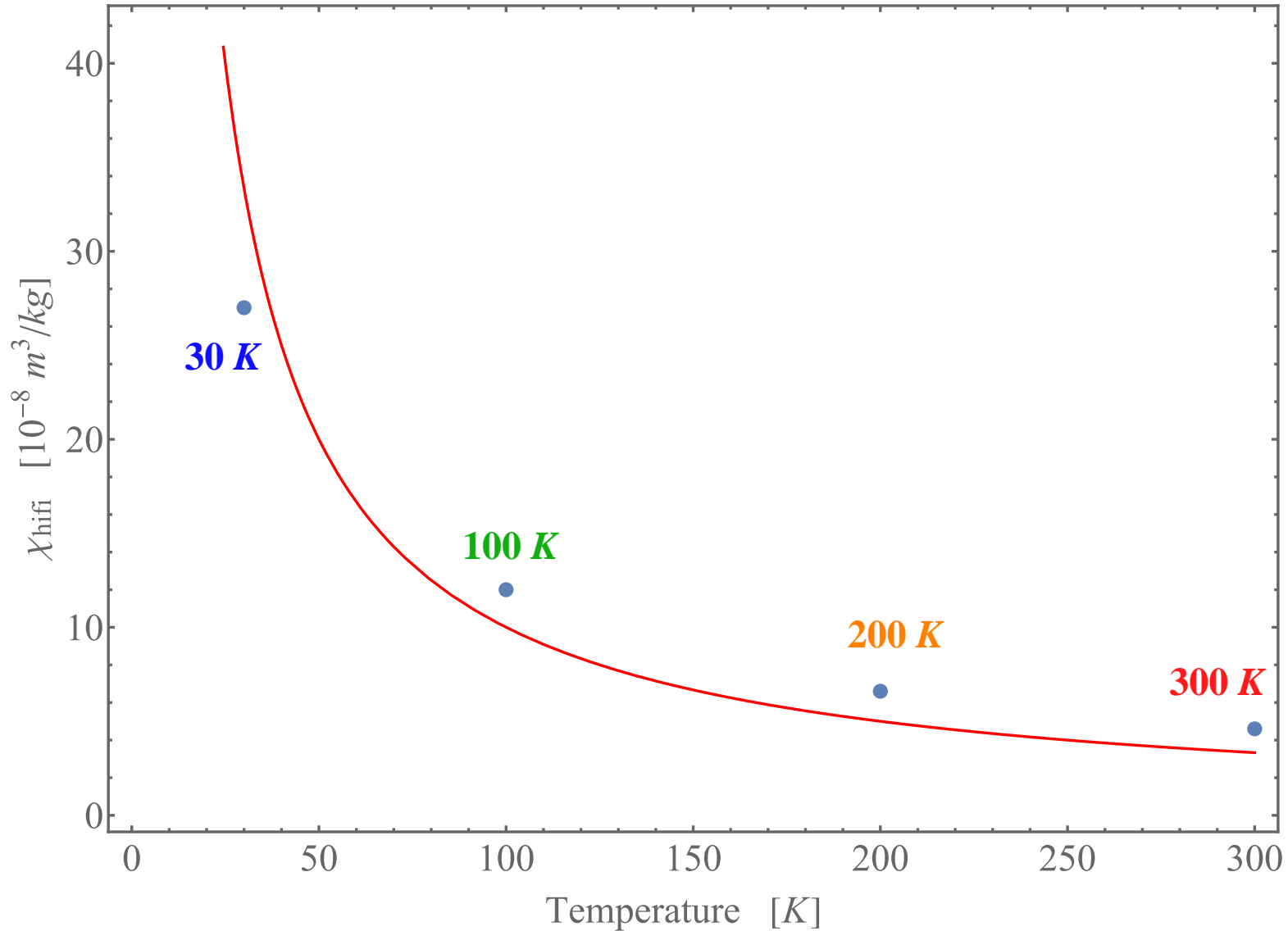
Ratios  $M_{rs}/M_s$  and  $H_{cr}/H_c$  are indicators of the magnetic grain size

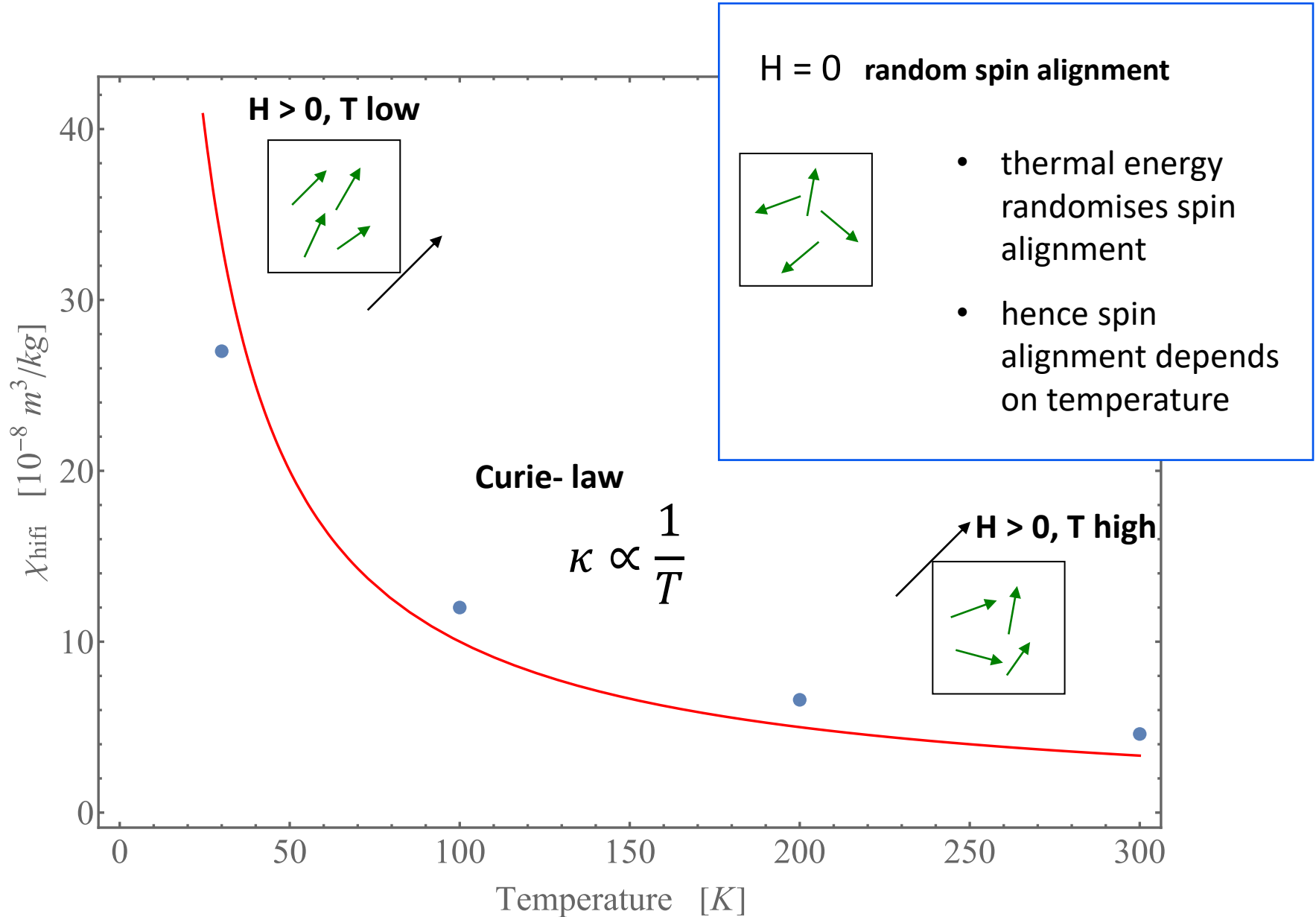




## Hysteresis







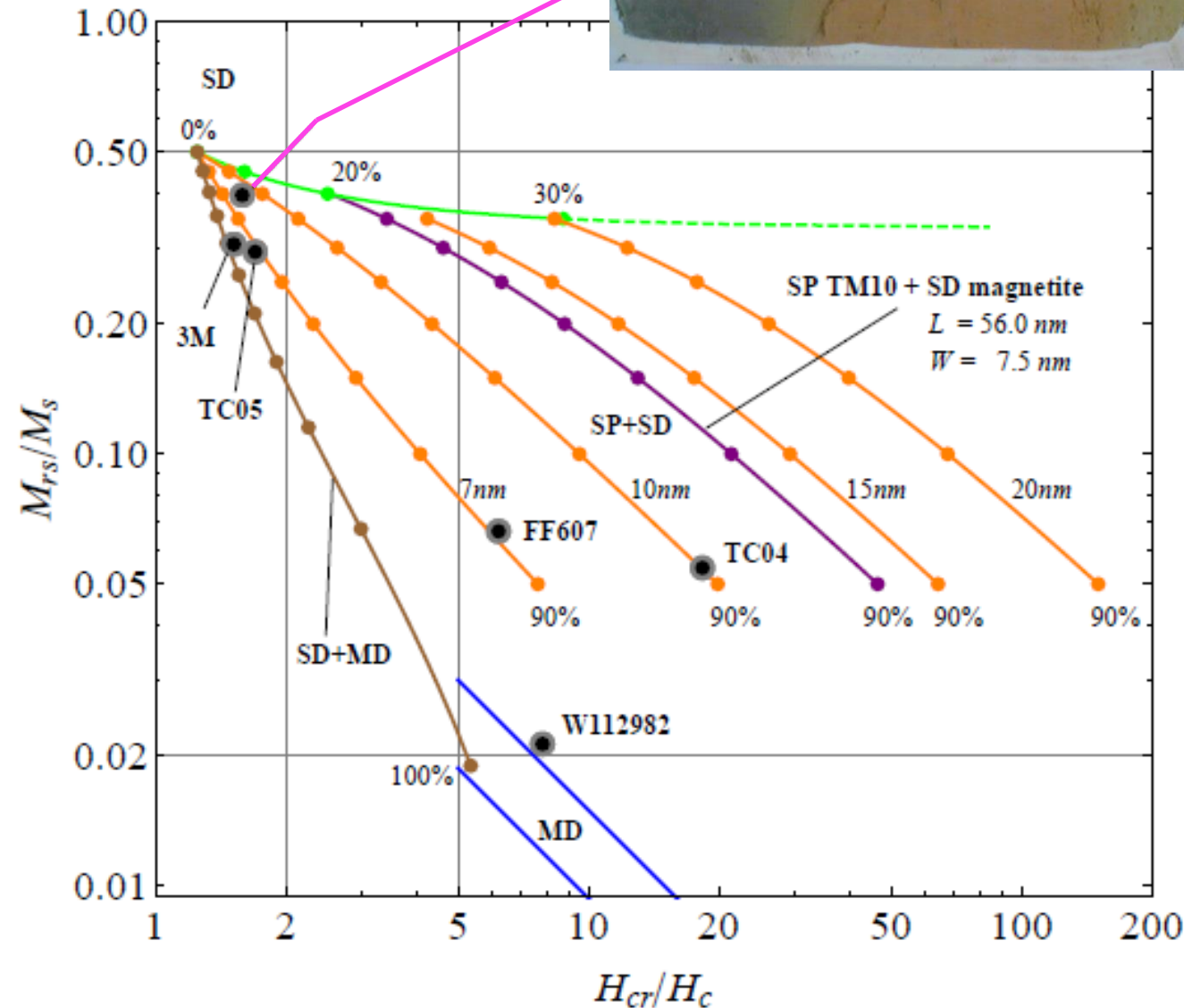


## Magnetic hysteresis



Day-Dunlop plot

for magnetite samples



Ratios  $M_{rs}/M_s$  and  $H_{cr}/H_c$  are indicators of the magnetic grain size

## Definition & Units

$$\vec{M} = \kappa \vec{H} \quad H [A/m] \text{ and } M [A/m] \rightarrow \kappa \text{ dimensionless, refers to volume}$$

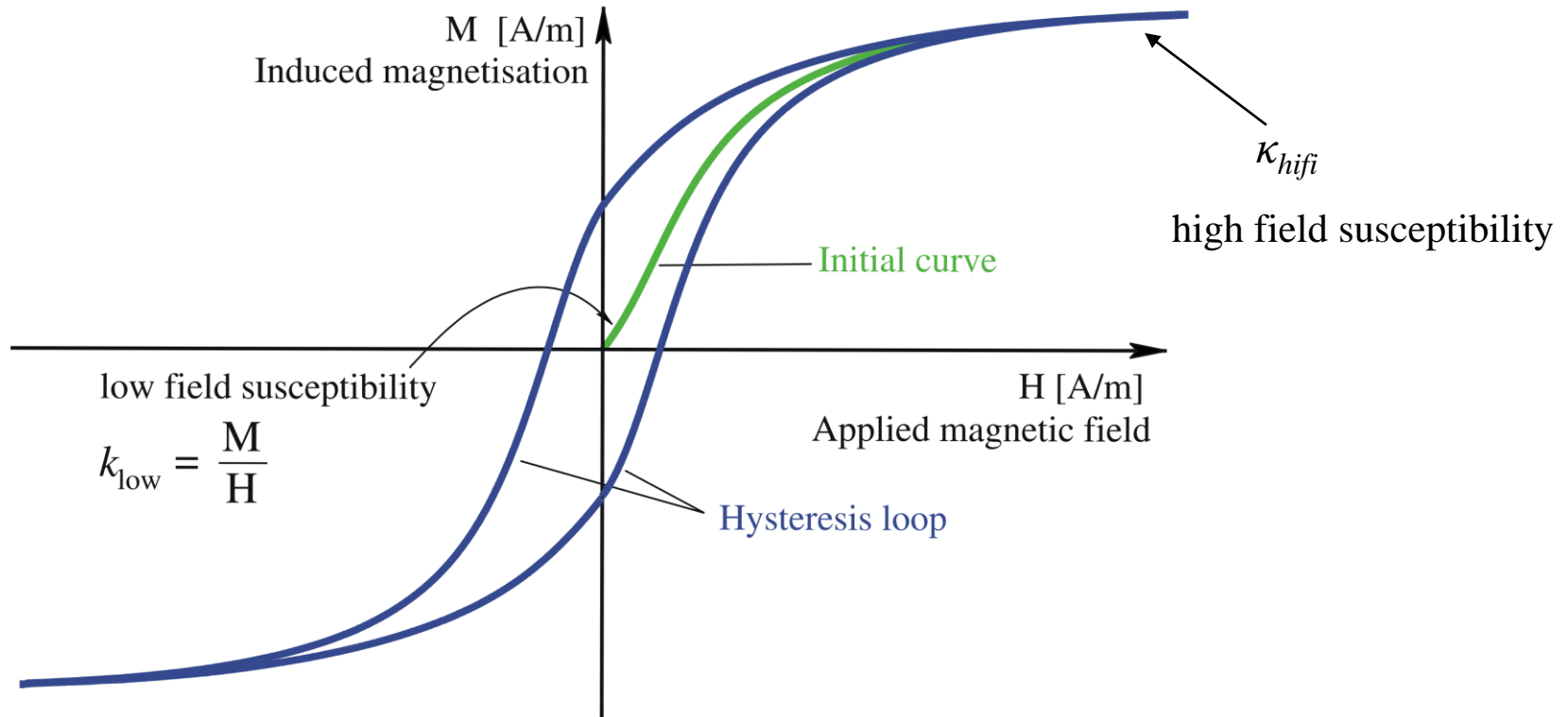
$$M_i = \kappa_{ij} H_j \quad 2^{\text{nd}} \text{ degree Tensor}$$

### For practical use

$$\text{Mass susceptibility} \quad \chi_{mass} = \frac{\kappa}{\rho} = \frac{\kappa}{m_{sample}} V_{measurement} \quad [m^3/kg]$$

$$\text{Molar susceptibility} \quad \chi_{molar} = M \cdot \chi_{mass} \quad [m^3/mol]$$

## DC susceptibility



Initial and high-field susceptibility are determined by fitting the  $M(H)$  curve.

General practice  $\kappa_{low}$  obtained from AC measurements, only  $\kappa_{hifi}$  used for interpretations.

## Susceptibility

### AC susceptibility

$$\vec{M} = \kappa \vec{H}$$

$$H_{ac} = H(t) = H_0 \cos(\omega t)$$

$$\kappa_{ac} = \frac{\partial M}{\partial H_{ac}}$$

$$\kappa_{ac} = \kappa' - i\kappa''$$

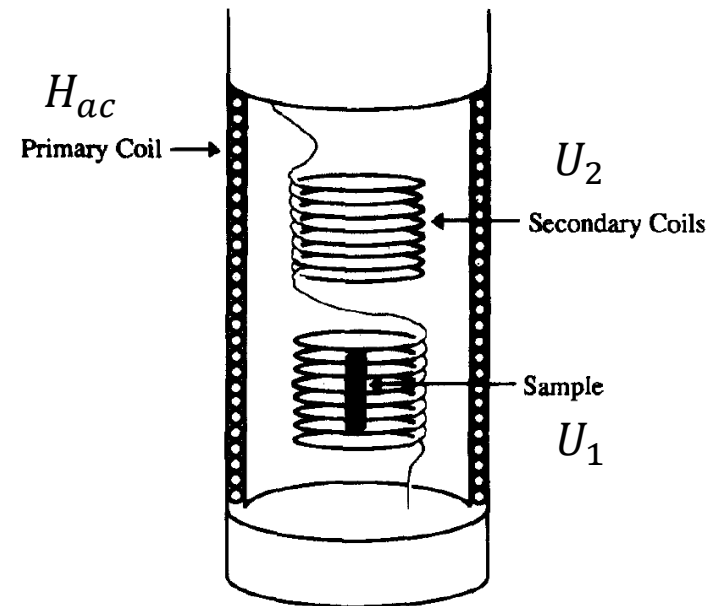
$$M(t) = \sum_{n=1}^{\infty} H_0^n (\kappa'_n \cos n\omega t + \kappa''_n \sin n\omega t)$$



for  $n = 1$

$$U(t) = c n\omega H_0 (\kappa'_1 \sin \omega t - \kappa''_1 \cos \omega t)$$

$$U(t) = -c \cdot \frac{dM(t)}{dt}$$



from Nikolo, *Am. J. Phys.* 63, 1995

$U$  measured with a phase separating lock-in amplifier  $\rightarrow \kappa'$  and  $\kappa''$  can be separated.

## AC susceptibility

### Real part

 $\chi'$ 

- Related to reversible magnetisation processes.
- Absorption of energy during magnetisation.
- Stays in phase with the driving oscillating field,
- Reflects the sensitivity of material to applied magnetising field  $H$ . “Magnetisability”
- is positive for antiferro-, ferro-, ferri-, paramagnetics
- is negative for diamagnetics

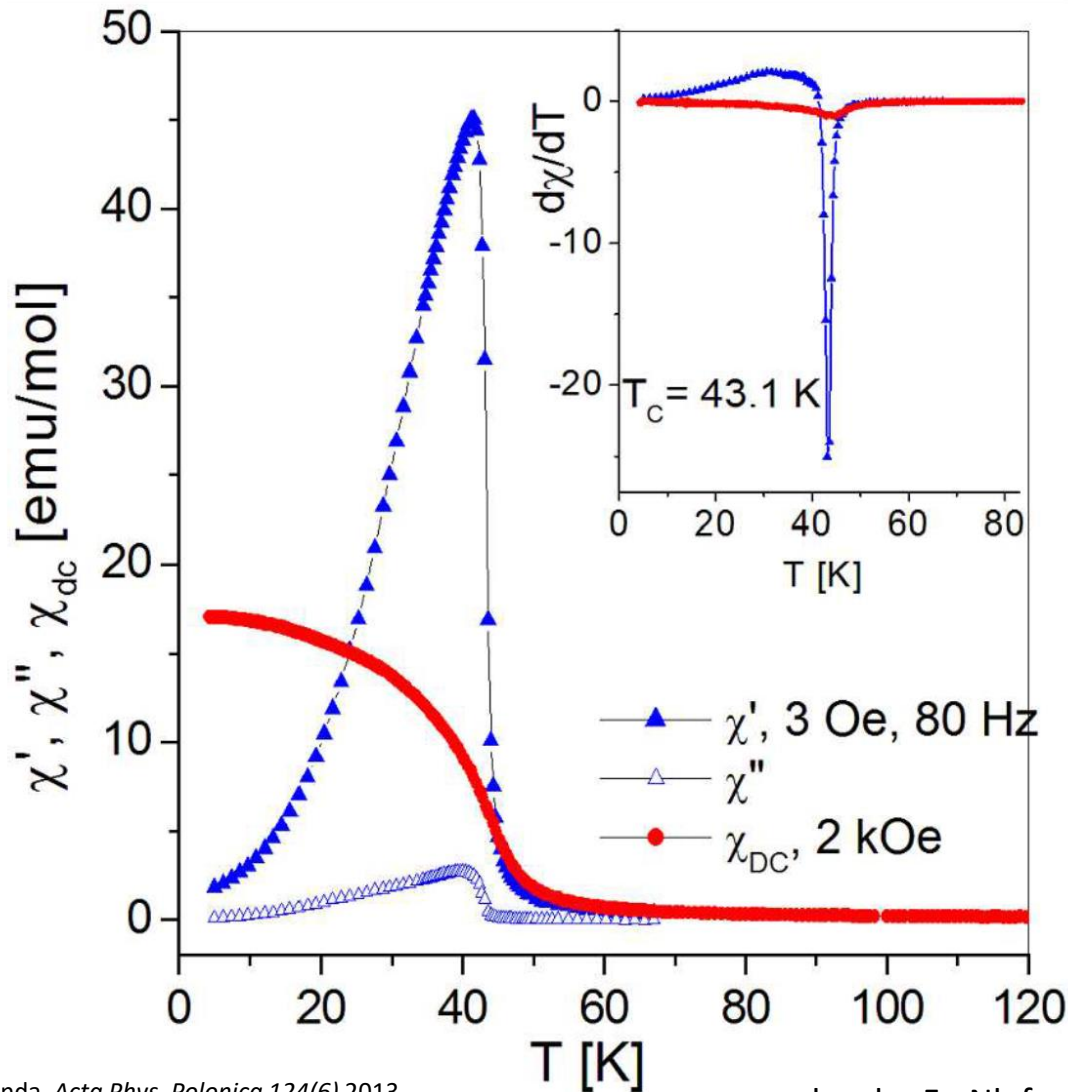
## AC susceptibility

### Imaginary part

$\chi''$

- Due to irreversible magnetisation changes
- Dissipation of energy during magnetisation, e.g. due to:
  - irreversible domain wall movements
  - relaxation of SP grains
  - Spin lattice relaxation in paramagnets
  - eddy currents in conducting materials
- May be zero or positive, but never negative.
- $\chi'' < \chi'$
- If  $\chi'' = 0 \rightarrow \chi_{ac} = \chi_{dc}$

## Susceptibility



## AC vs. DC susceptibility

Balanda, *Acta Phys. Polonica* 124(6) 2013,  
Pinkowicz et al., *Dalton Trans.*, 2009,

molecular Fe-Nb ferromagnet with a Curie temperature well below room temperature

## Instruments measuring $\kappa_{AC}$

Producer	$T$ [K]	$H_{ac}$ [A/m]	$f$ [kHz]	$H_{DC-bias}$ [mT]
Bartington	73-1123	0.2	0.456 & 4.56	-
Agico	81-973	5-750	0.976, 3.904, 15.6	-
QD	0.5-1000	8-800	0.0001-1	0.5-7000



Bulk, anisotropy,  $\chi(T)$ ,  $\chi(f)$ ,  $\chi(H)$



## Instruments measuring $\kappa_{AC}$

Producer	$T$ [K]	$H_{ac}$ [A/m]	$f$ [kHz]	$H_{DC-bias}$ [mT]
Bartington	73-1123	0.2	0.456 & 4.56	-
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[www.bartington.com](http://www.bartington.com)

## Instruments measuring $\kappa_{AC}$

Producer	$T$ [K]	$H_{ac}$ [A/m]	$f$ [kHz]	$H_{DC-bias}$ [mT]
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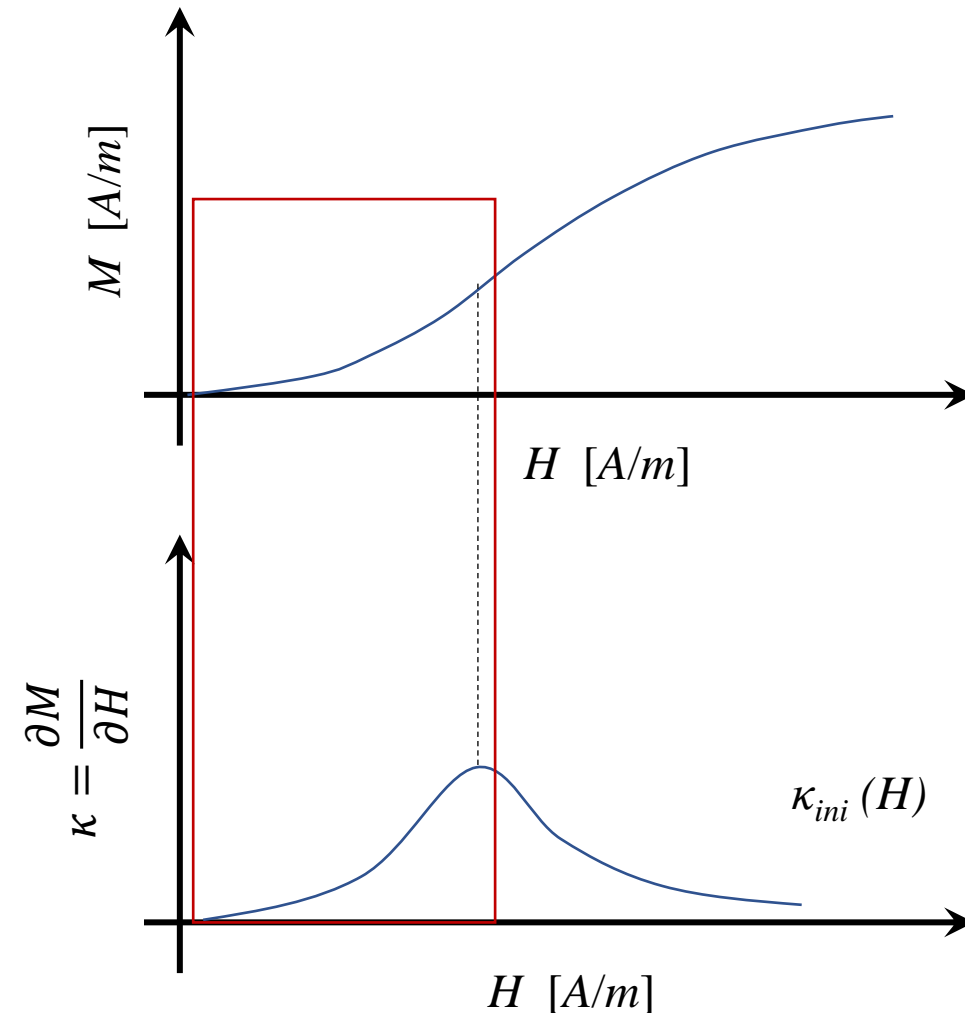
Bartington	73-1123	0.2	0.456 & 4.56	-
Agico	81-973	5-750	0.976, 3.904, 15.6	-
QD	0.5-1000	8-800	0.0001-1	0.5-7000



DC in function of  $T, H$ ,  
 Anisotropy in function of  $H$   
 AC  $\chi'$ ,  $\chi''$  in function of  $T, H, f$

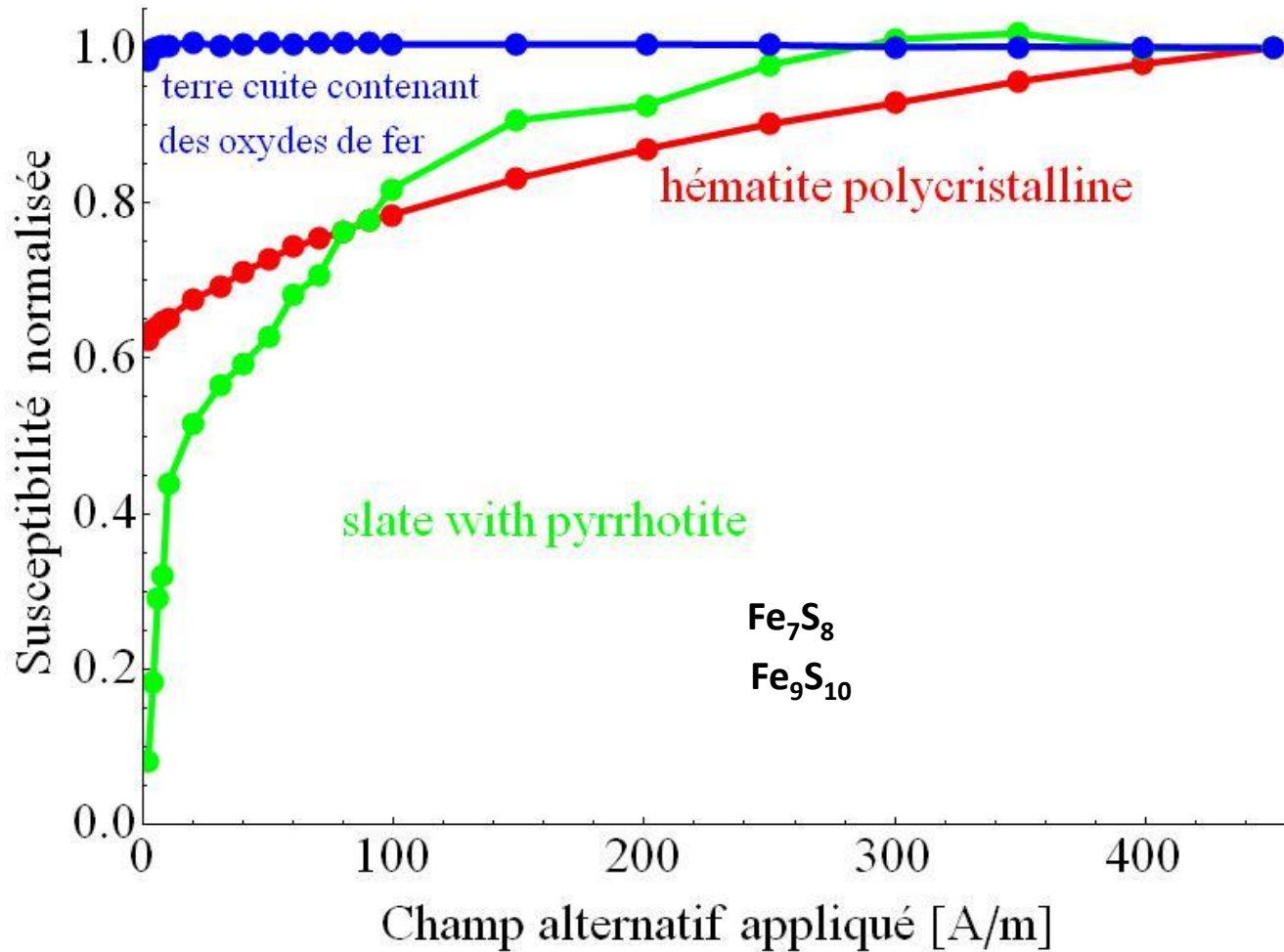
## Field dependence

magnetic mineral identification

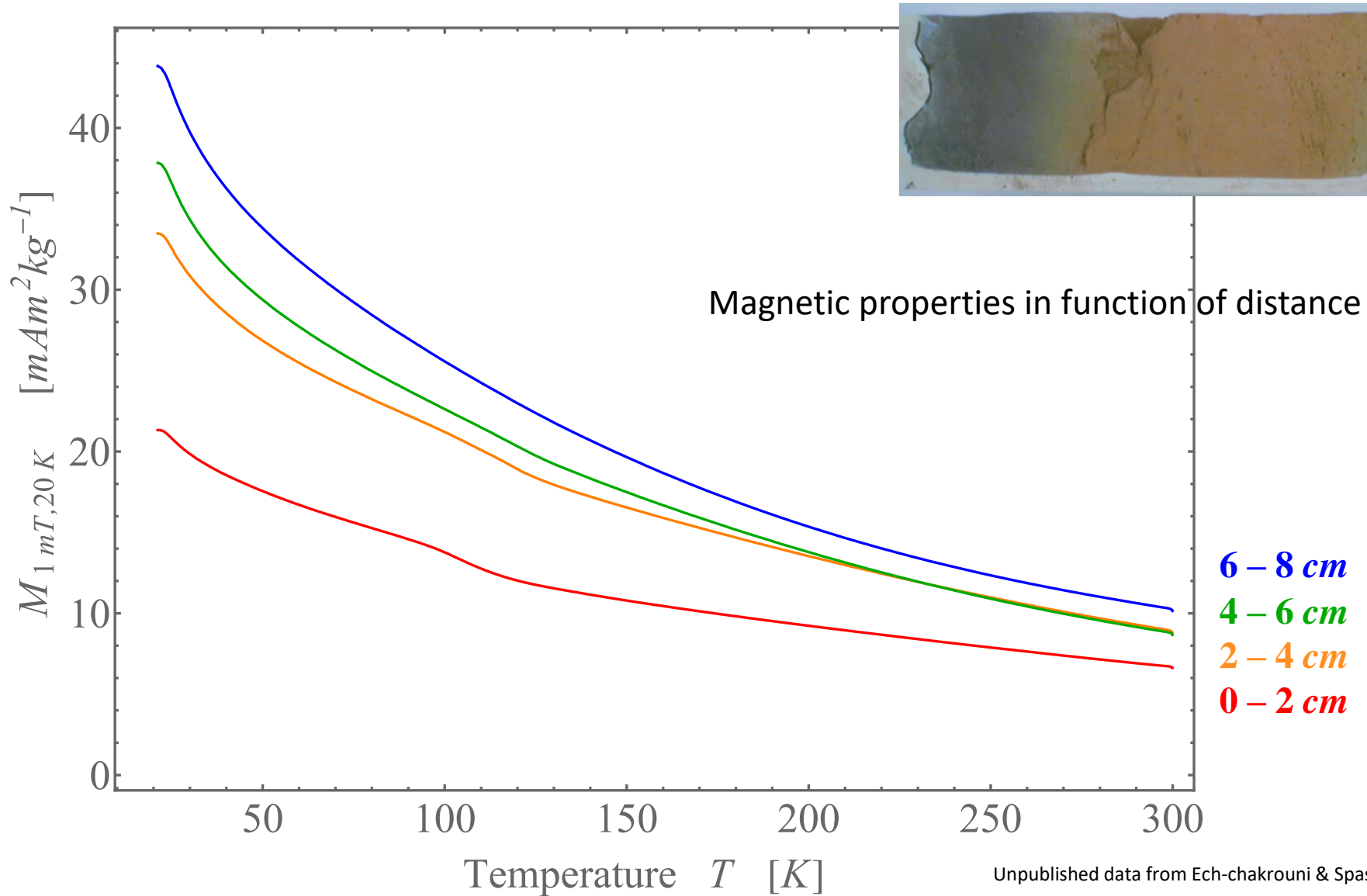


- small fields  $< 800$  A/m  
(in reversible region of hysteresis loop)
- Initial slope changes are different for different magnetic minerals

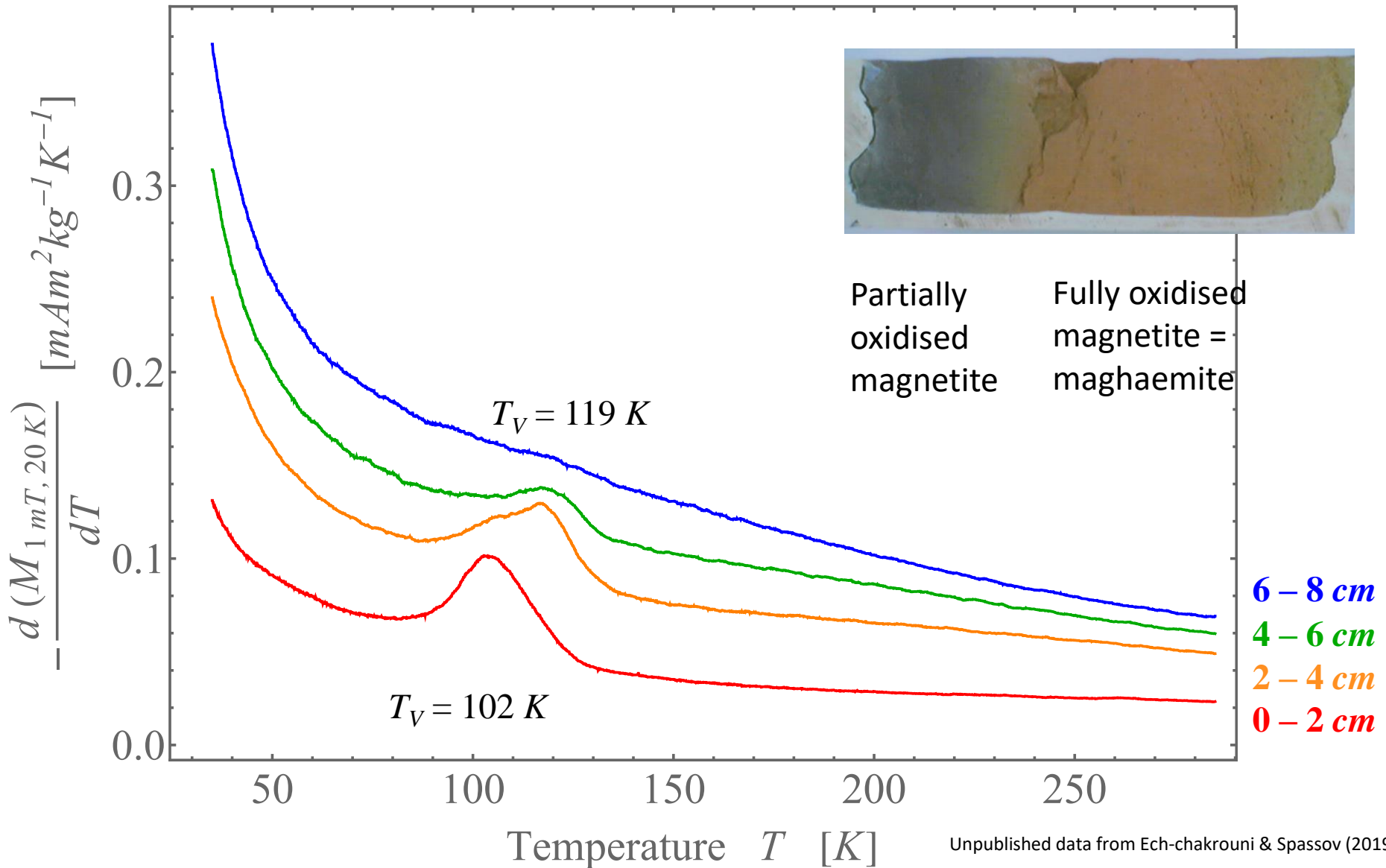
### Field dependence



Unpublished data Hus & Spassov (2006)

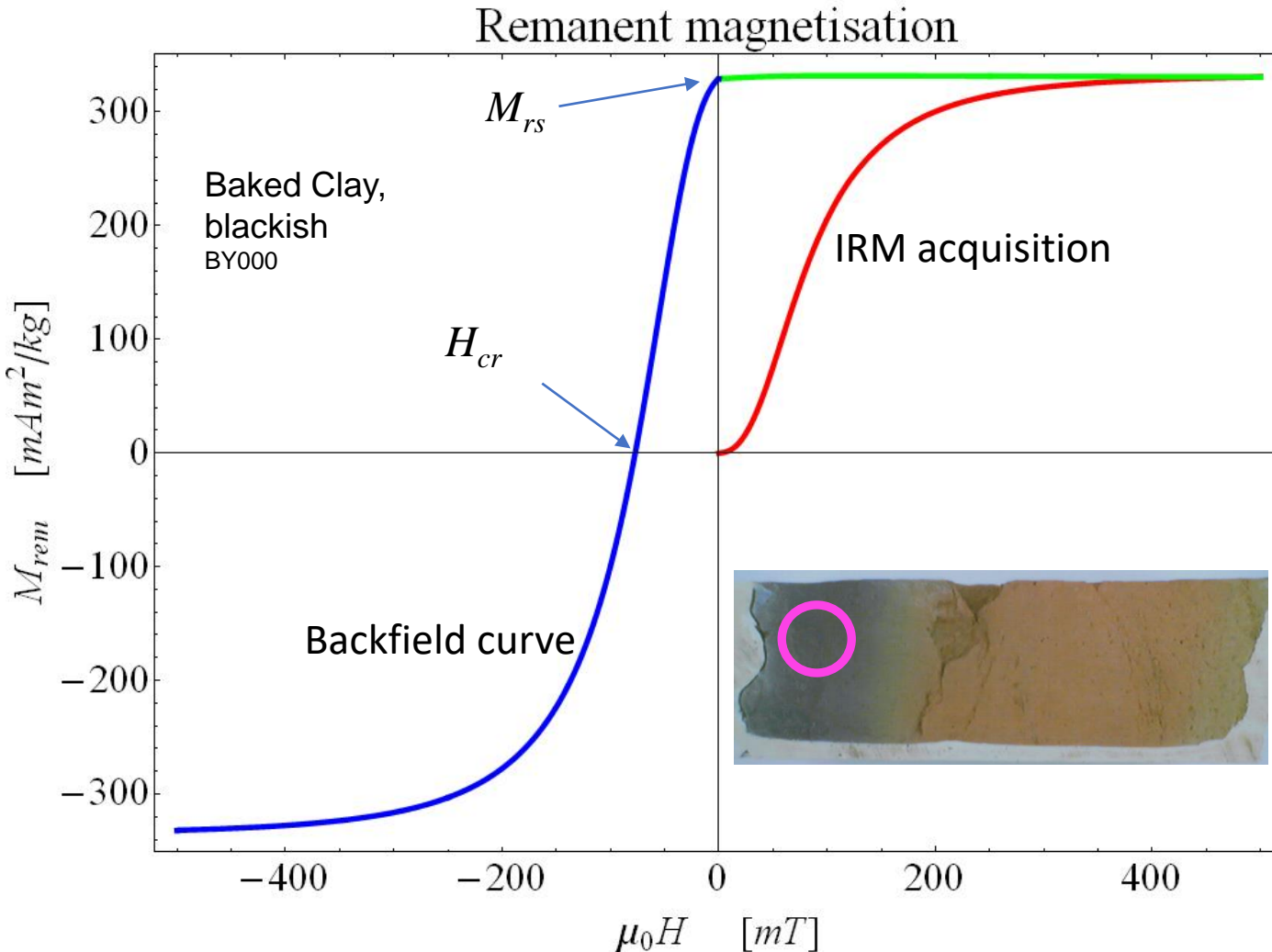


Unpublished data from Ech-chakrouni & Spassov (2019)



Isothermal remanent magnetisation

Steady field magnetisation



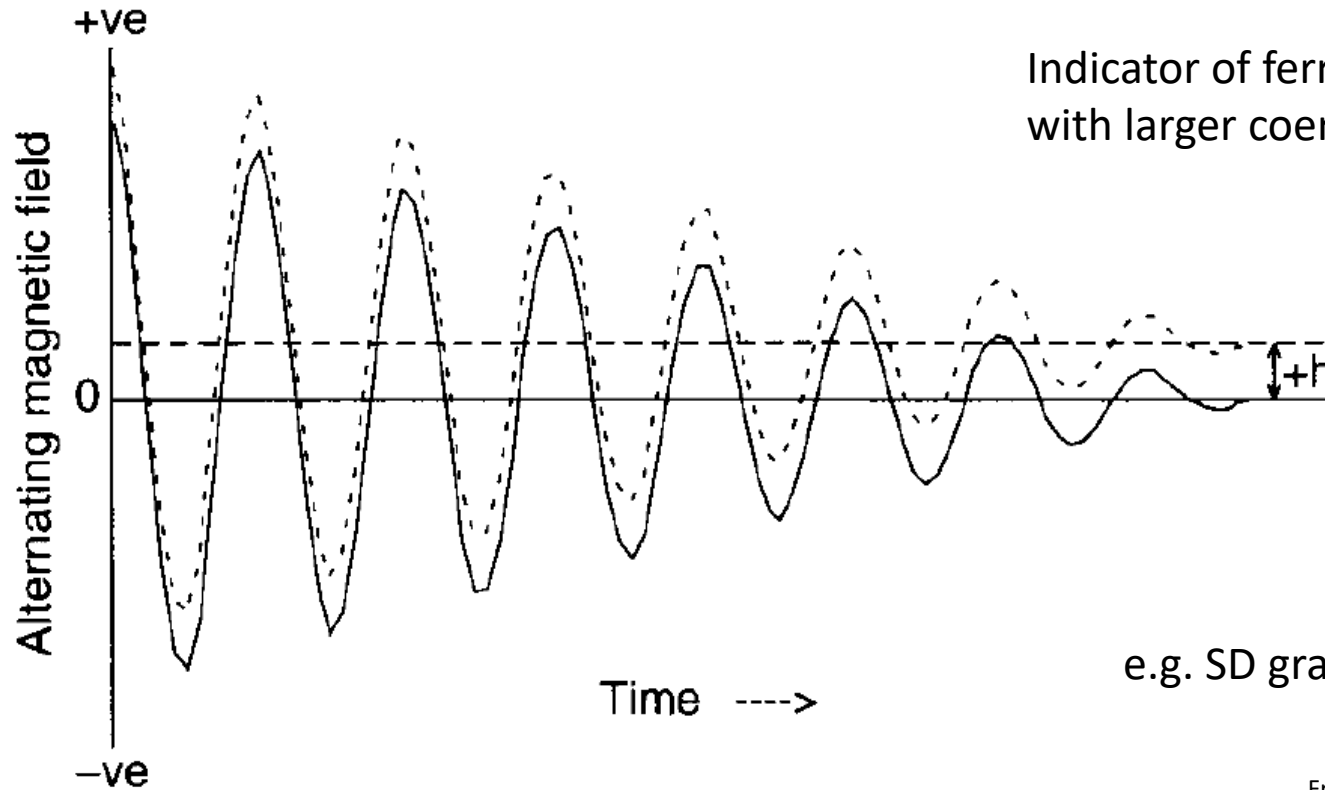
S-ratio

$$\frac{|IRM_{-300mT}|}{M_{rs}}$$

Ratios < 1 indicative for presence of high-coervivity minerals

# Anhyysteretic remanent magnetisation

Steady field magnetisation and alternating field demagnetisation at once



Indicator of ferrimagnetic grains with larger coercive forces

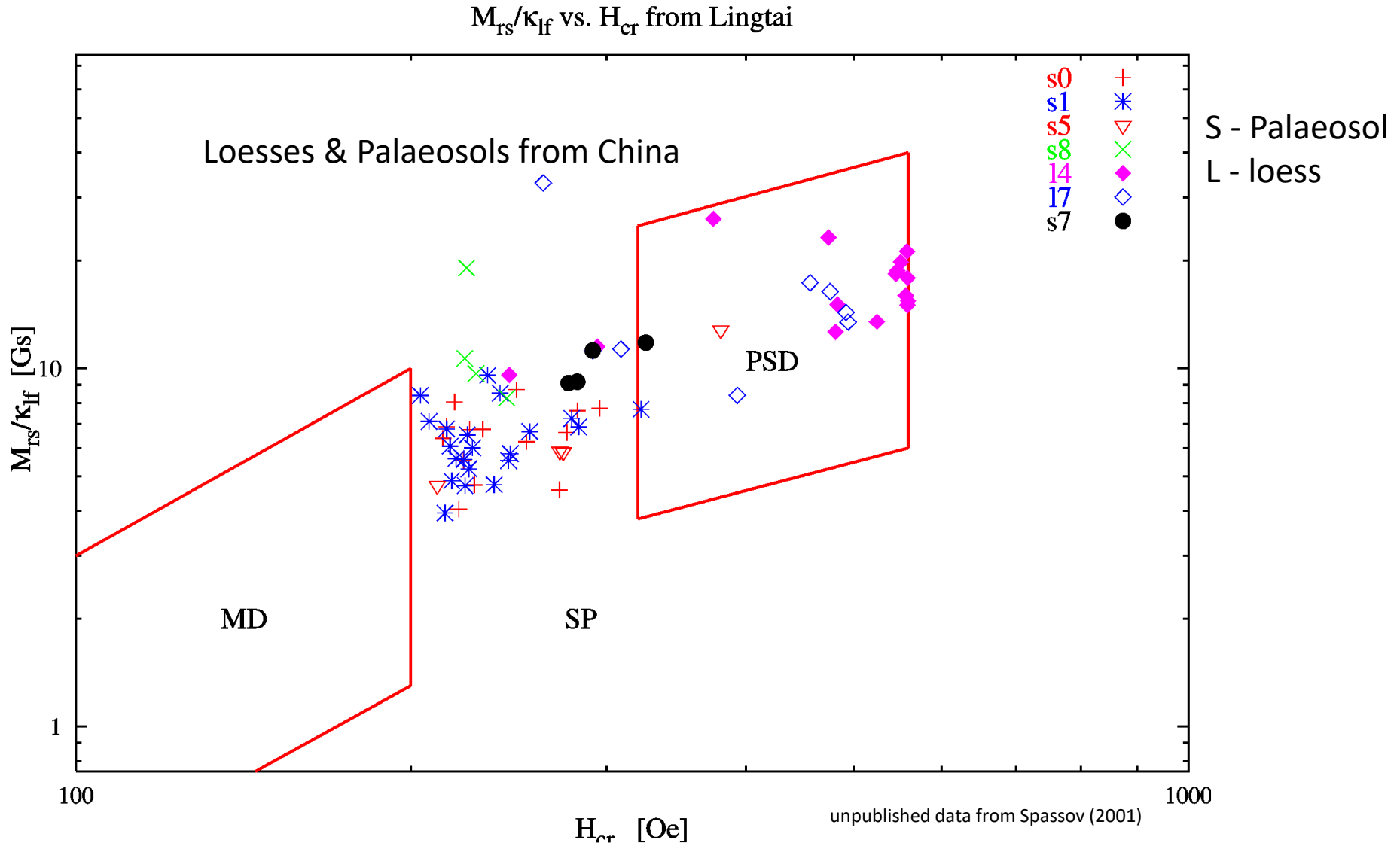
e.g. SD grains of magnetite

From Evans & Heller (2003)



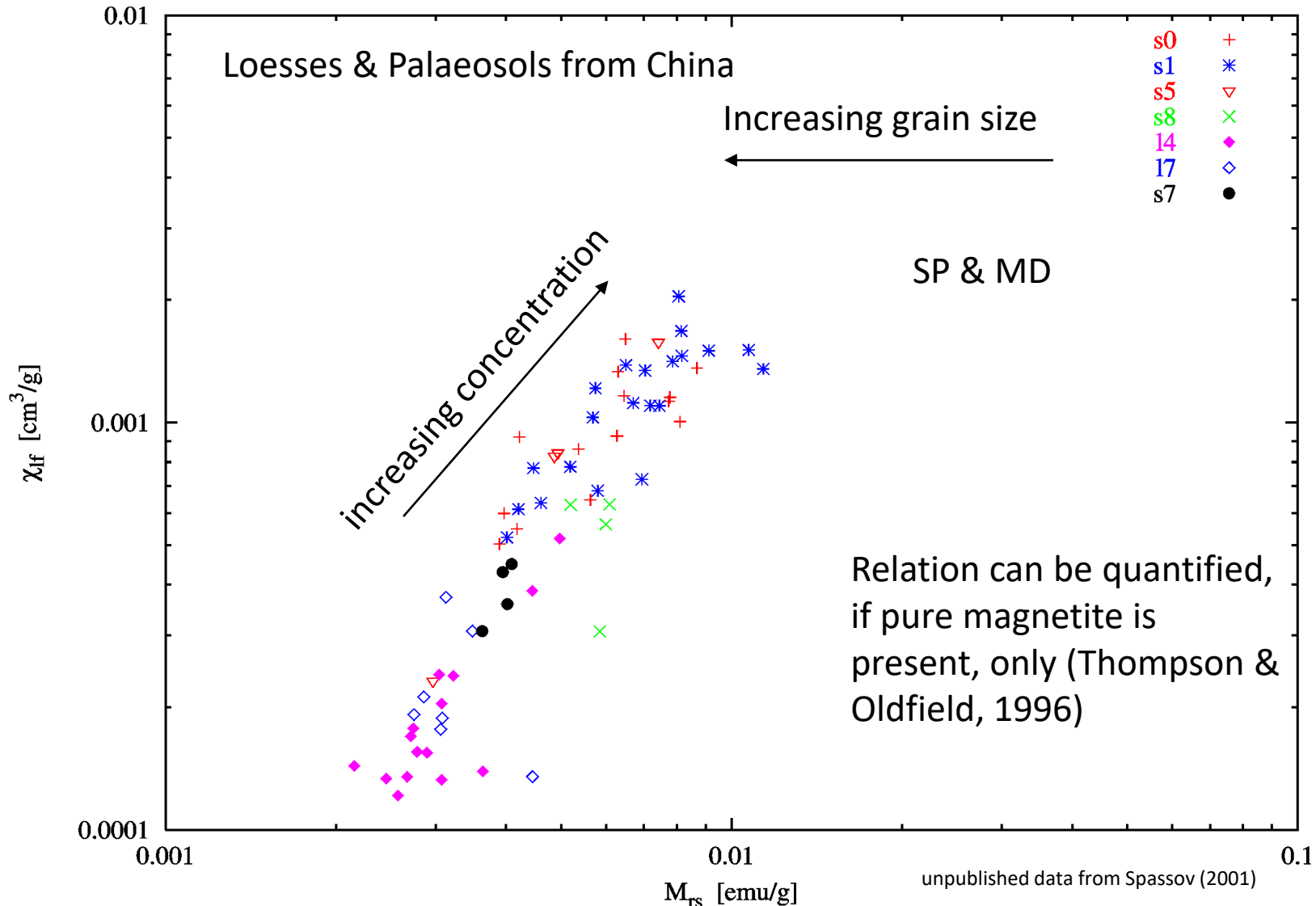
# Normalised SIRM vs remanent coercive force

grain size

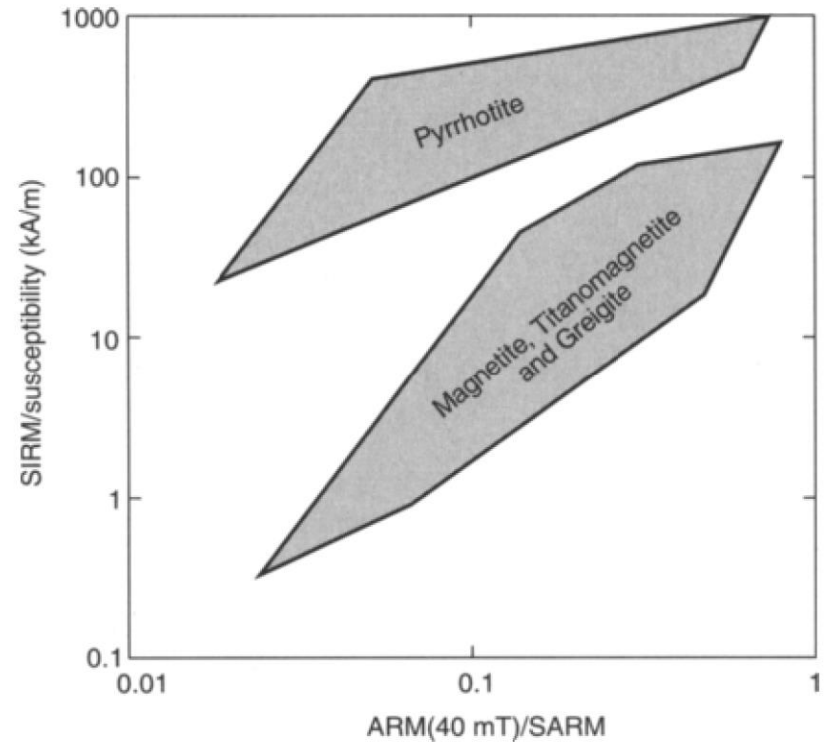
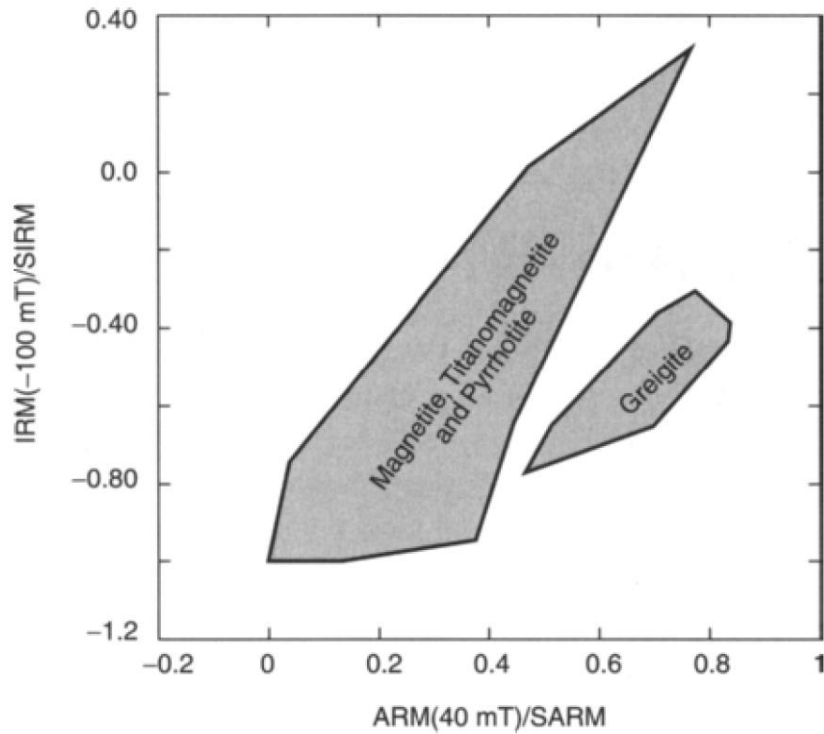


## Saturation remanence vs. susceptibility

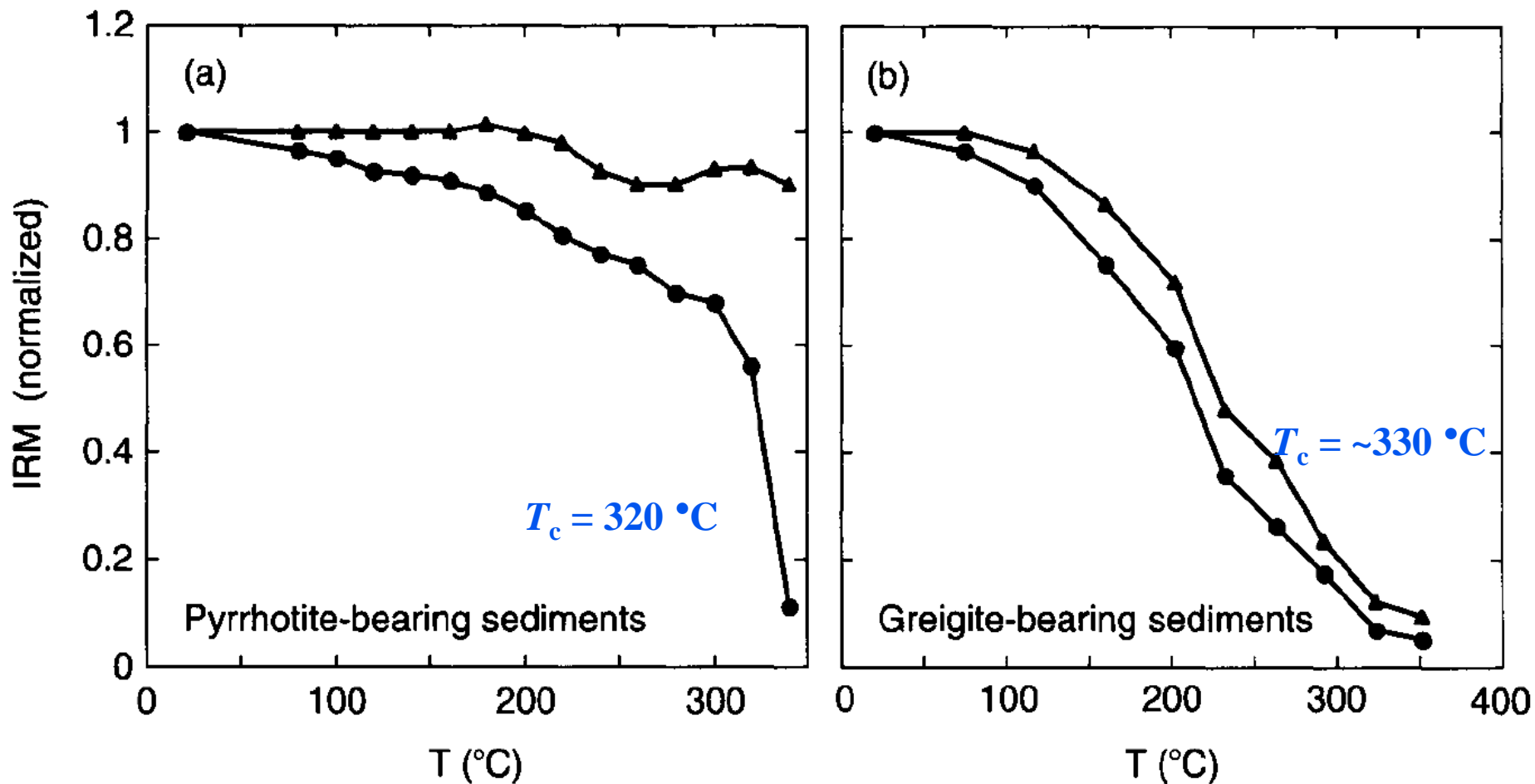
### Grain size & concentration



## Backfield IRM vs ARM

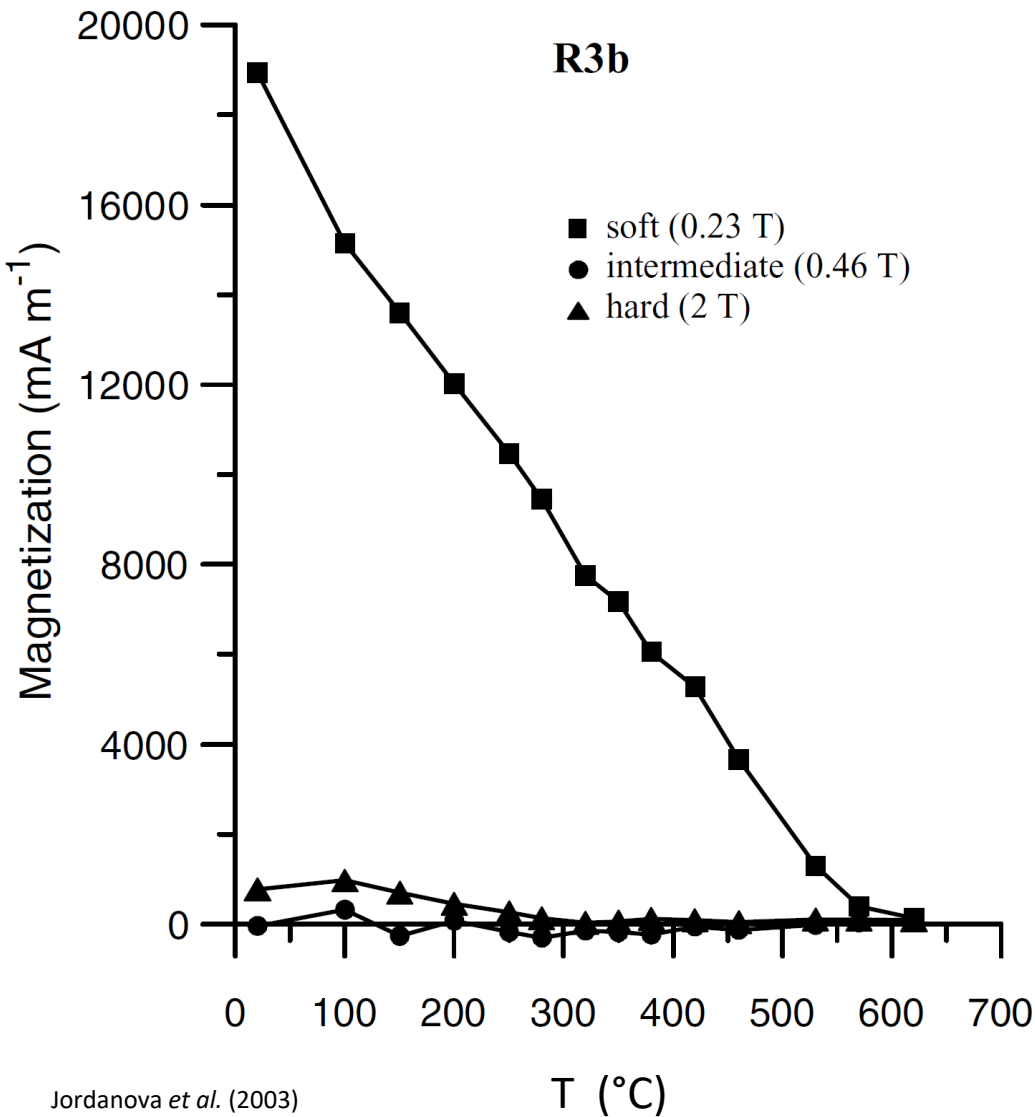


From Evans & Heller (2003)



From Evans & Heller (2003)

# Thermal demagnetisation of IRM



Jordanova et al. (2003)

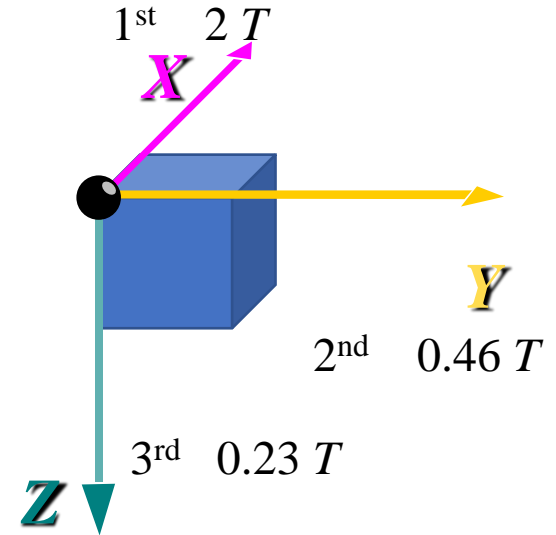
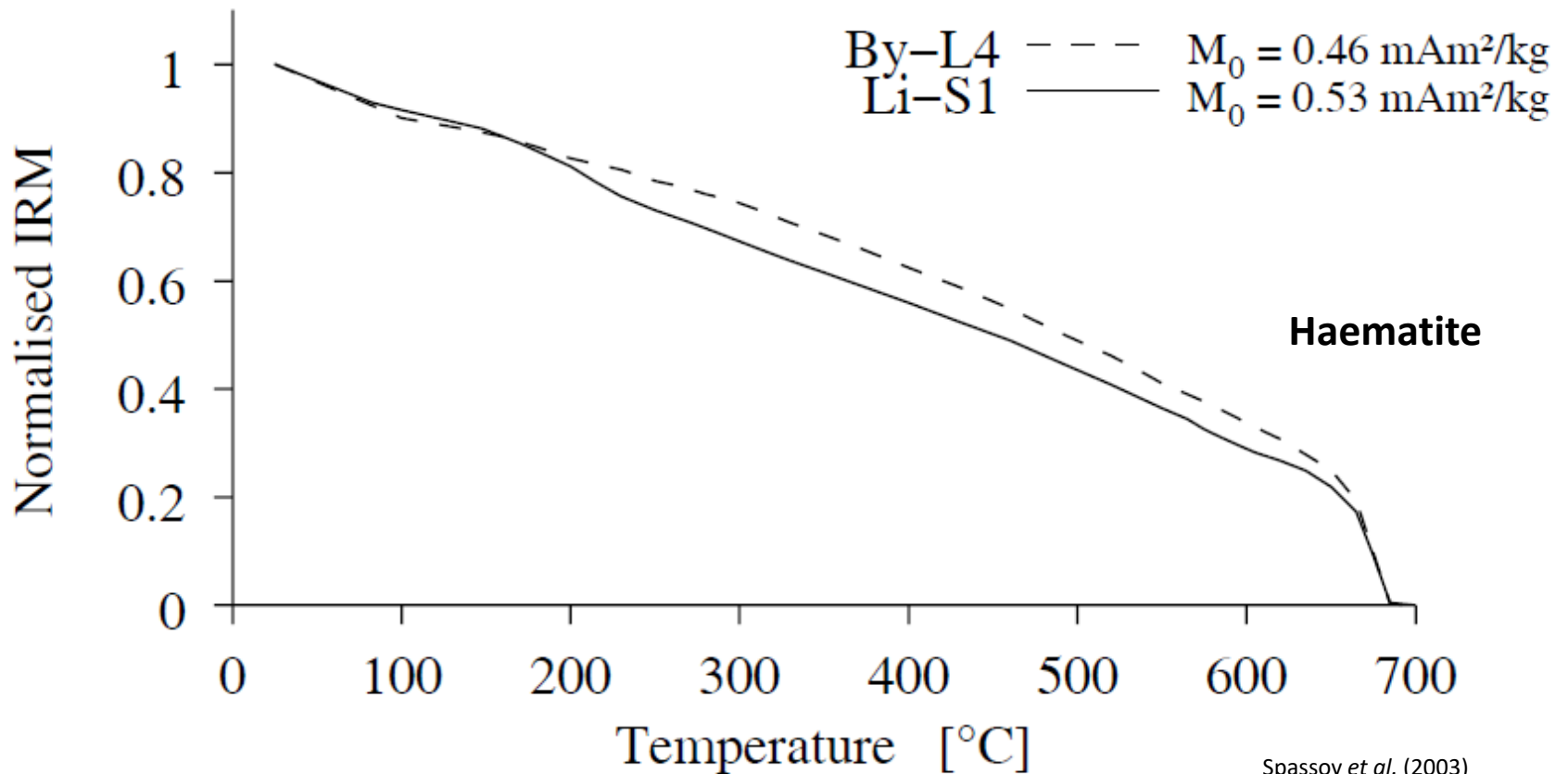


Table 5.1 Maximum coercivities and blocking temperatures for some common ferromagnetic minerals

Ferromagnetic mineral	Maximum coercivity [T]	Maximum blocking temperature [ $^{\circ}\text{C}$ ]
Magnetite	0.3	575
Maghemite	0.3	$\approx 350$
Titanomagnetite ( $\text{Fe}_{3-x}\text{Ti}_x\text{O}_4$ ):		
$x=0.3$	0.2	350
$x=0.6$	0.1	150
Pyrrhotite	0.5–1	325
Hematite	1.5–5	675
Goethite	$> 5$	80–120

Lowrie (2007)

High coercivity component: 280 – 1500 mT



Spassov *et al.* (2003)

1. Magnetise in strong field, e.g. 2 T,
2. demagnetise with alternating fields

## Decay of IRM

### Remanent magnetisation decays over time

$$M(t) = M_0 e^{-t/\tau} + M_{eq} (1 - e^{-t/\tau}) \quad \text{for SD grains}$$

$$M_{eq} = M(t \rightarrow \infty)$$

$$M_0 = M(t = 0)$$

$$\tau = f(V, M_s, H_k, H_0) \quad \text{relaxation time}$$

$H_k$  – micro-coercivity assuming shape anisotropy

$H_0$  – external field

$V$  – lognormal distribution of volumes

Small grains, e.g. 30 – 40 nm magnetite/maghaemite or haematite loose their remanence quickly

Larger grains, i.e. single domain and multidomain do practically not loose their remanence.

# Decay of IRM

